

# Design of Linear CMOS RF Power Amplifiers

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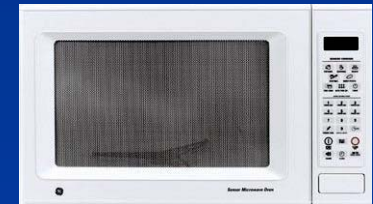
LCI –UFSC – Florianópolis, SC  
28 de outubro de 2010



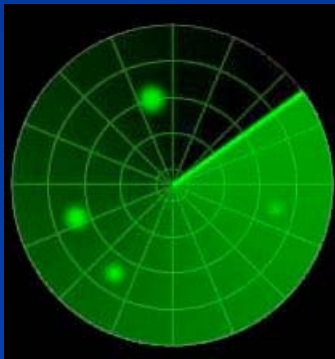
# Outline

- Introduction
- Linear Power Amplifier (PA) basics
- Efficiency enhancement: Dynamic Supply
- Conclusion

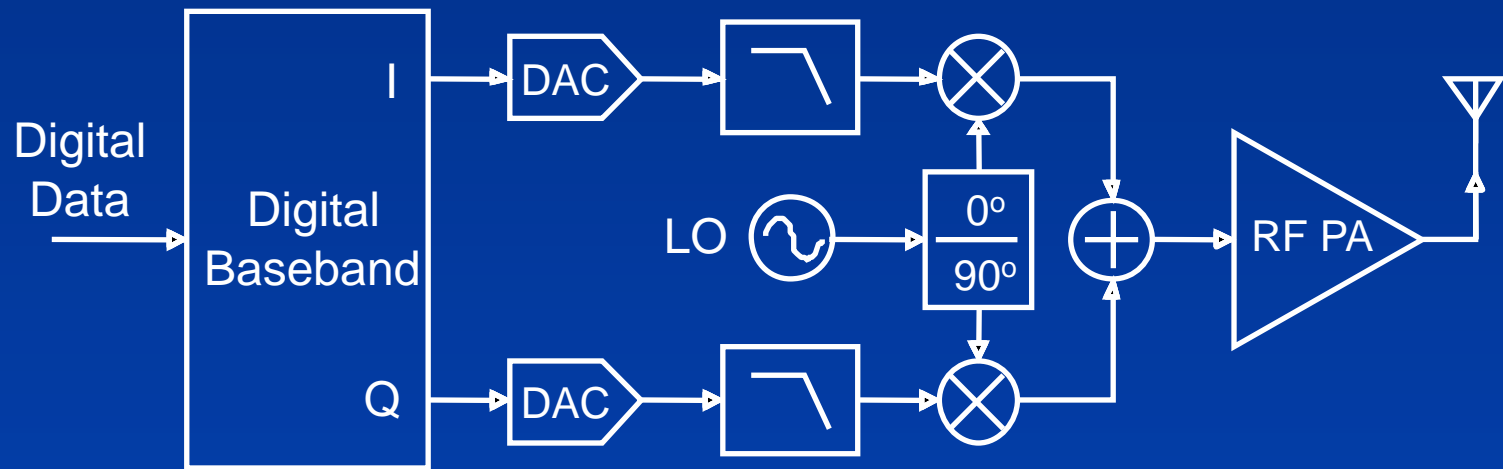
# Introduction



## RF Applications

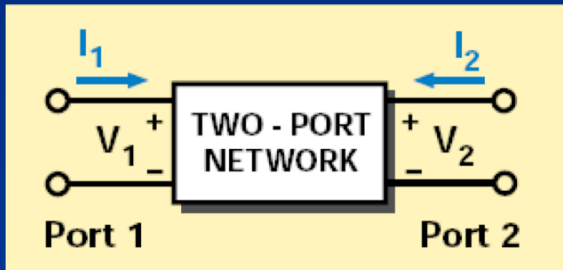


# RF Transceiver



Direct conversion transmitter

# Two-port representation/S-parameters



## Admittance

$$I_1 = y_{11} \cdot V_1 + y_{12} \cdot V_2$$

$$I_2 = y_{21} \cdot V_1 + y_{22} \cdot V_2$$

$$y_{11} = \left. \frac{I_1}{V_1} \right|_{V_2=0}$$

$$y_{12} = \left. \frac{I_1}{V_2} \right|_{V_1=0}$$

$$y_{21} = \left. \frac{I_2}{V_1} \right|_{V_2=0}$$

$$y_{22} = \left. \frac{I_2}{V_2} \right|_{V_1=0}$$

$$V_1 = z_{11} \cdot I_1 + z_{12} \cdot I_2$$

$$V_2 = z_{21} \cdot I_1 + z_{22} \cdot I_2$$

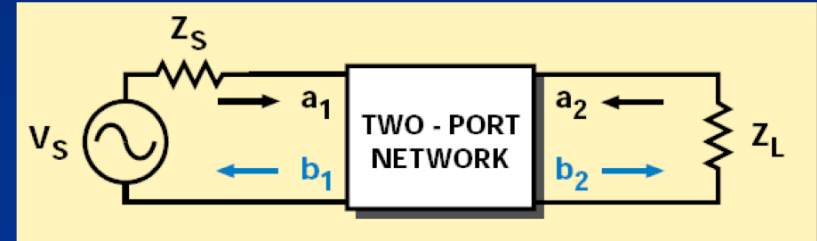
$$z_{11} = \left. \frac{V_1}{I_1} \right|_{I_2=0}$$

$$z_{12} = \left. \frac{V_1}{I_2} \right|_{I_1=0}$$

$$z_{21} = \left. \frac{V_2}{I_1} \right|_{I_2=0}$$

$$z_{22} = \left. \frac{V_2}{I_2} \right|_{I_1=0}$$

## Impedance



## Scattering

$$b_1 = s_{11} \cdot a_1 + s_{12} \cdot a_2$$

$$b_2 = s_{21} \cdot a_1 + s_{22} \cdot a_2$$

$$s_{11} = \left. \frac{b_1}{a_1} \right|_{a_2=0}$$

$$s_{12} = \left. \frac{b_1}{a_2} \right|_{a_1=0}$$

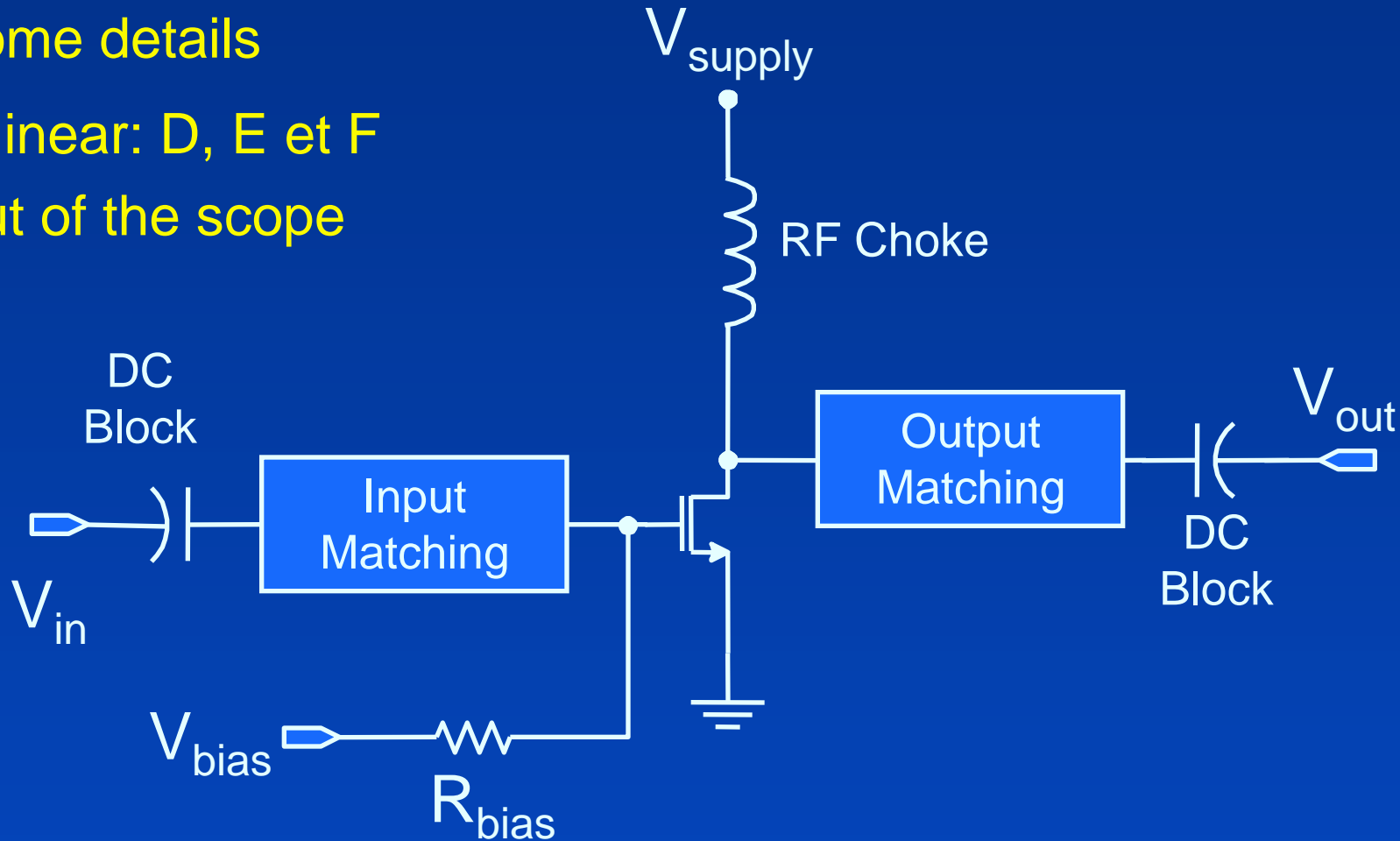
$$s_{21} = \left. \frac{b_2}{a_1} \right|_{a_2=0}$$

$$s_{22} = \left. \frac{b_2}{a_2} \right|_{a_1=0}$$

S-parameters are easier to measure. No need of neither short nor open circuits.

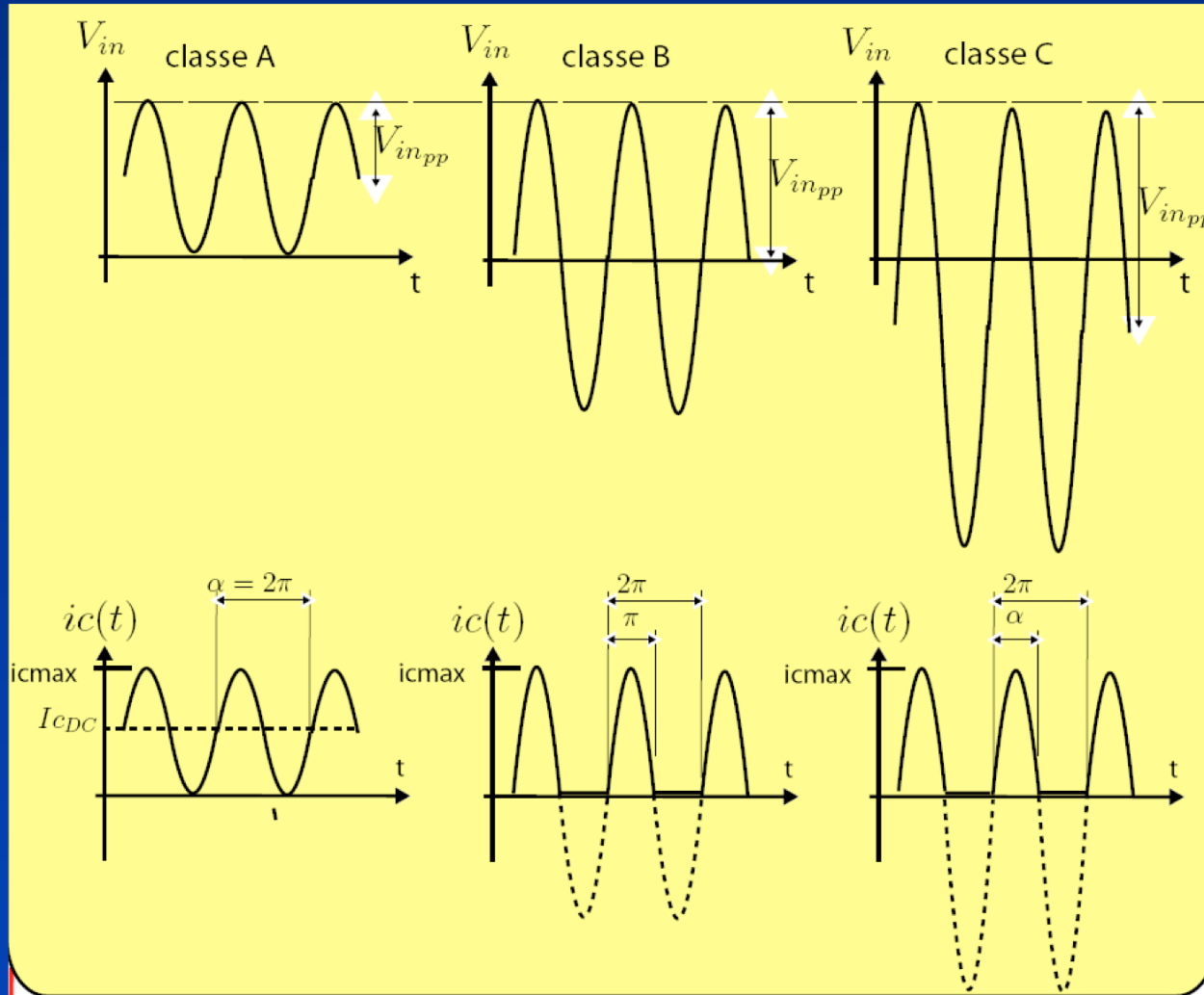
# PA Classes

- Linear classes: A, AB, B et C
  - some details
- Non linear: D, E et F
  - out of the scope



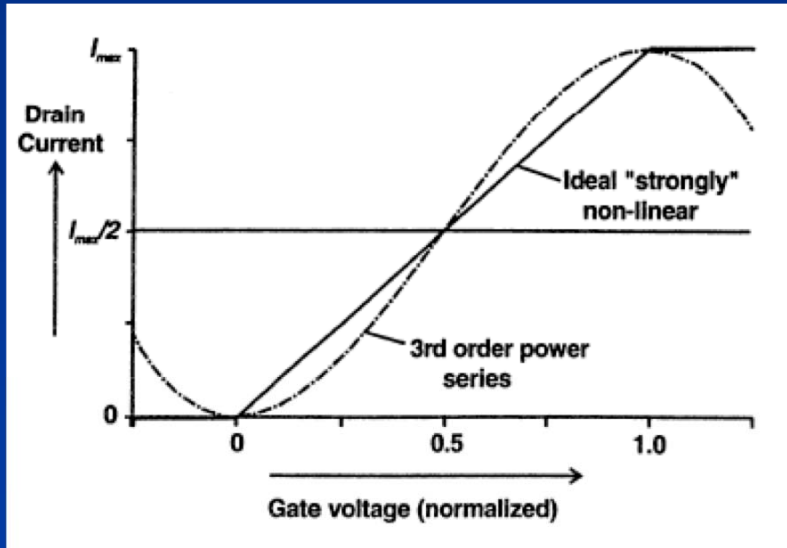
# Linear classes

conduction angle  $\alpha$  decreases  $\rightarrow$

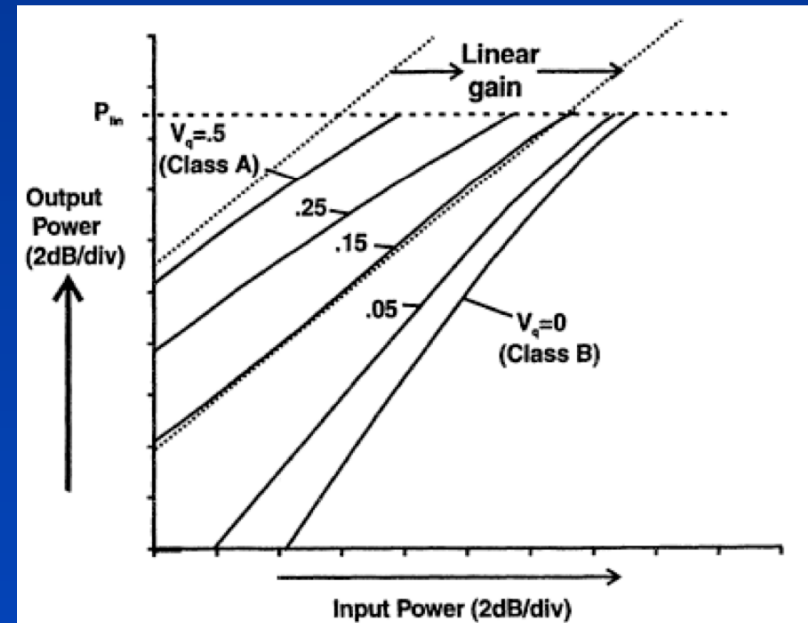


# Linear classes - comparison

## Weak-strong non-linear model\*



## Gain linearity\*



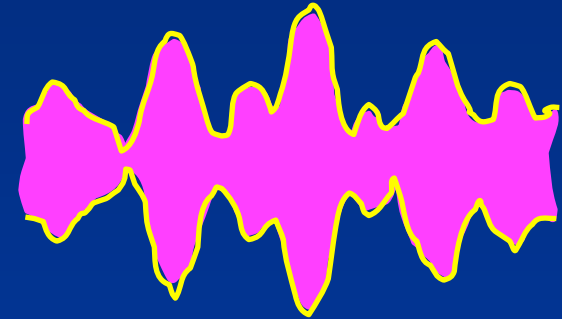
\*From Cripps [2]



# Class choice according to application

- Constant envelope modulation (GSM):
  - high efficiency PA (switched PA classes)
  - linearity not important
- Variable envelope modulation (IS-95, UMTS, WLAN):
  - linearity very important
    - Linear PA + efficiency enhancement technique
    - high efficiency PA + linearization technique

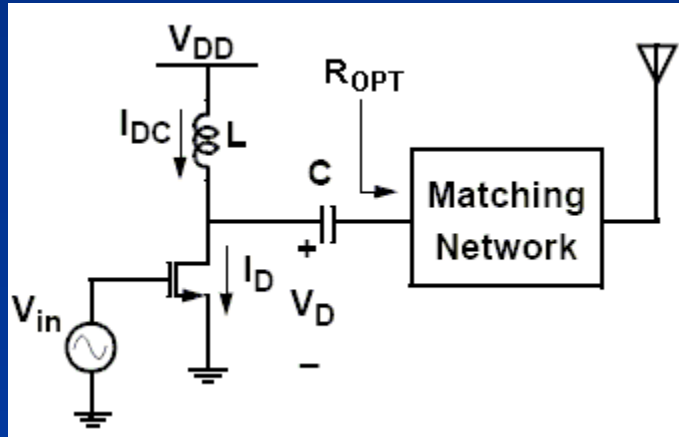
# WLAN 802.11a/g



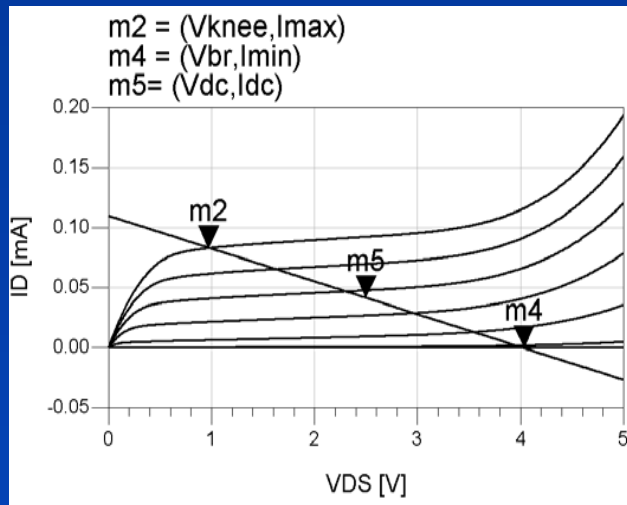
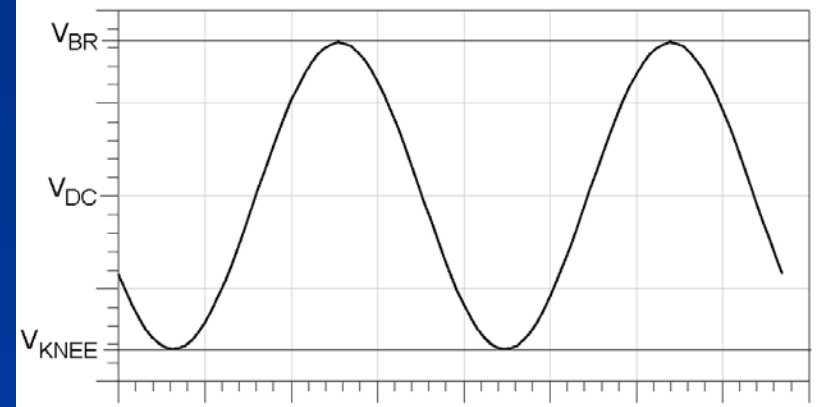
- Enveloppe variable
- large PAPR (17dB,  $\sqrt{52}$  )
- Requires a high linearity PA

**Class A PA**

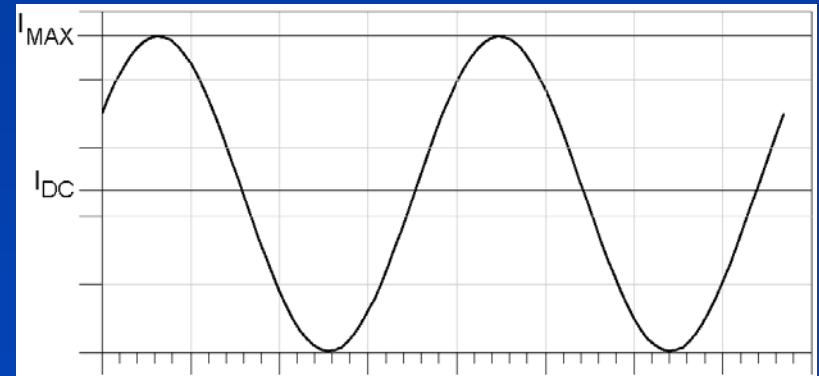
# Class A PA



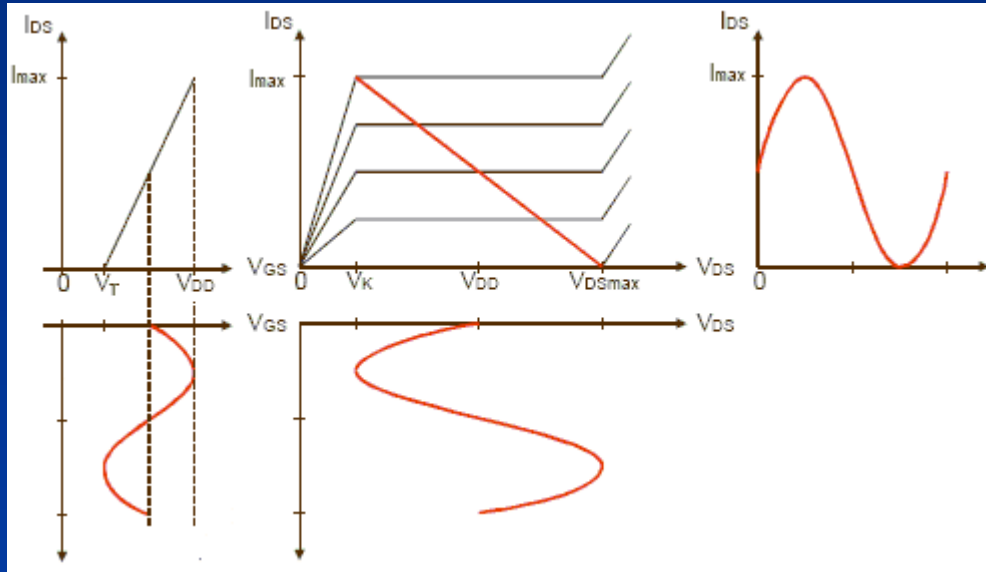
## Drain voltage



## Drain current



# Class A PA – Output Power I



$$V_{DC} = \frac{1}{2}(V_{BR} + V_{KNEE}) \quad I_{DC} = \frac{1}{2}I_{MAX}$$

If output voltage and  $R_{OPT}$  are known:

$$P_{OUT\_MAX} = \frac{V_{eff}^2}{R_{OPT}} \quad V_{eff} = \frac{V_{PP}}{2 \cdot \sqrt{2}}$$

$$P_{OUT\_MAX} = \frac{\left(\frac{V_{PP}}{2 \cdot \sqrt{2}}\right)^2}{R_{OPT}} = \frac{V_{PP}^2}{8 \cdot R_{OPT}}$$

If current and  $R_{OPT}$  are known:

$$P_{OUT\_MAX} = R_{OPT} \cdot I_{eff}^2 \quad I_{eff} = \frac{I_{MAX}}{2 \cdot \sqrt{2}}$$

$$P_{OUT\_MAX} = R_{OPT} \cdot \left(\frac{I_{MAX}}{2 \cdot \sqrt{2}}\right)^2 = R_{OPT} \cdot \frac{I_{MAX}^2}{8}$$

$$V_{PP} = V_{BR} - V_{KNEE}$$

$$P_{OUT\_MAX} = \frac{1}{8} \cdot \frac{(V_{BR} - V_{KNEE})^2}{R_{OPT}}$$

# Class A PA – Output power II

If output voltage and current are known:

$$V_{eff} = \frac{V_{PP}}{2 \cdot \sqrt{2}}$$

$$P_{OUT\_MAX} = V_{eff} \cdot I_{eff}$$

$$I_{eff} = \frac{I_{MAX}}{2 \cdot \sqrt{2}}$$

$$P_{OUT\_MAX} = \frac{V_{PP}}{2 \cdot \sqrt{2}} \cdot \frac{I_{MAX}}{2 \cdot \sqrt{2}} = \frac{V_{PP} \cdot I_{MAX}}{8}$$

$$P_{OUT\_MAX} = \frac{1}{8} \cdot (V_{BR} - V_{KNEE}) \cdot I_{MAX}$$

$$P_{OUT\_MAX} = \frac{1}{4} (V_{BR} - V_{KNEE}) \cdot I_{DC}$$

$$P_{OUT\_MAX} = \frac{1}{4} (V_{DC} - V_{KNEE}) \cdot I_{MAX}$$

$$P_{OUT\_MAX} = \frac{1}{2} (V_{DC} - V_{KNEE}) \cdot I_{DC}$$

Expressions for  $R_{OPT}$ :

$$R_{OPT} = \frac{(V_{DC} - V_{KNEE})}{I_{DC}}$$

$$R_{OPT} = \frac{(V_{DC} - V_{KNEE})^2}{2 \cdot P_{OUT\_MAX}}$$

$$R_{OPT} = \frac{V_{BR} - V_{KNEE}}{I_{MAX}}$$

$$R_{OPT} = \frac{1}{8} \cdot \frac{(V_{BR} - V_{KNEE})^2}{P_{OUT\_MAX}}$$

# Considerations on $R_{OPT}$

- It is necessary to guarantee that the desired maximum output power can be delivered to the load:
  - limited supply voltage
  - transistor non idealities

# Transistor sizing

For a given **output power**, if  $V_{BR}$  and  $V_{KNEE}$  of the transistor are known:

1. Determine  $R_{opt}$   $\longrightarrow R_{OPT} = \frac{1}{8} \cdot \frac{(V_{BR} - V_{KNEE})^2}{P_{OUT\_MAX}}$
2. Calculate necessary  $I_{MAX}$   $\longrightarrow I_{MAX} = \frac{(V_{BR} - V_{KNEE})}{R_{OPT}}$
3. The transistor must be designed for  $I_{MAX}$   $\longrightarrow I_D = \frac{1}{2} \cdot k' \cdot \frac{W}{L} \cdot (V_{GS} - V_T)^2$
4. Calculate  $W/L$   $\longrightarrow \frac{W}{L} = \frac{2 \cdot I_{MAX}}{k' \cdot (V_{GS} - V_T)^2}$
5. Verification with simulator

# Choice of VGS and W/L

- Case 1 – integrated transceiver
  - input capacitance
  - input signal swing
- Case 2 – stand-alone PA
  - No constraints, VGS and W/L can be chosen so as to maximize linearity or efficiency



# PA stability

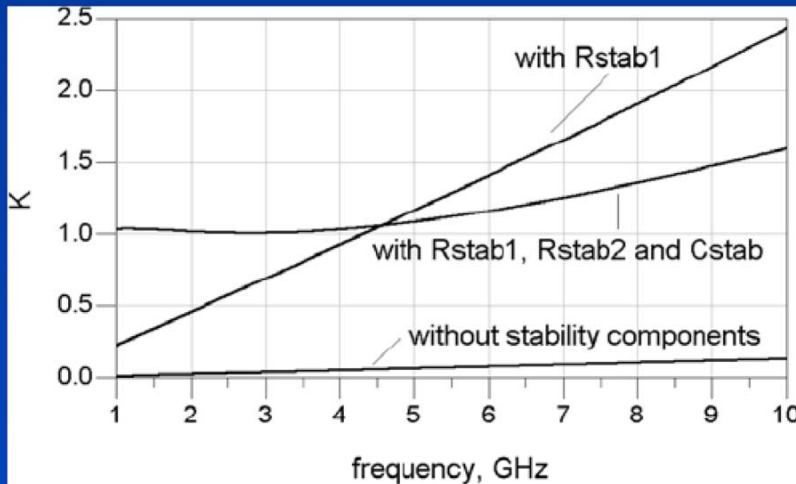
K factor > 1 (Rollet [3])

$$K = \frac{1 + |D|^2 - |s_{11}|^2 - |s_{22}|^2}{2|s_{12}s_{21}|}$$

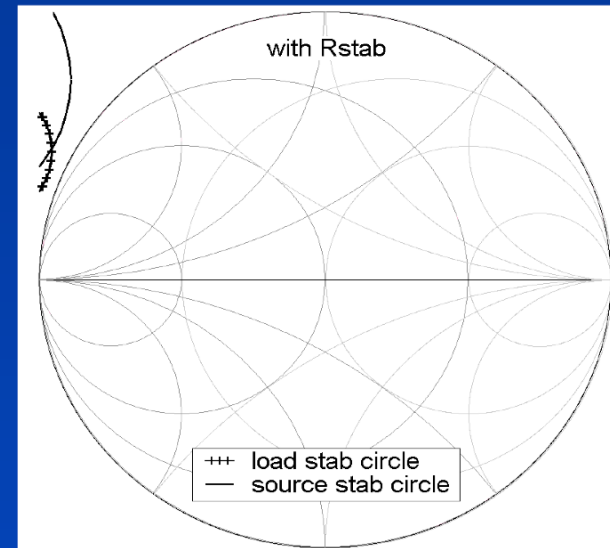
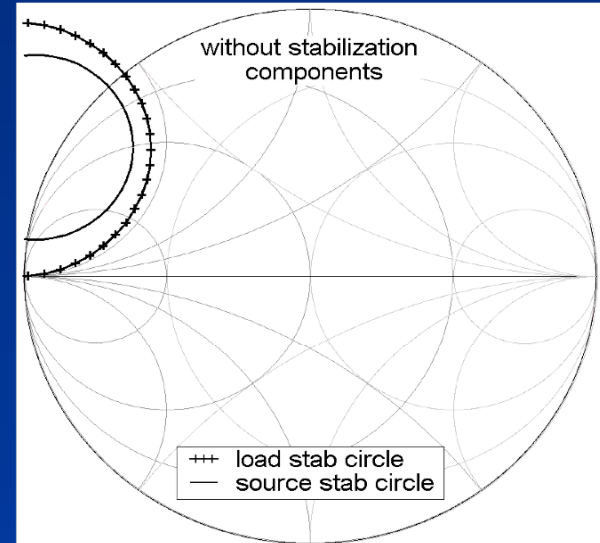
$$D = s_{11}s_{22} - s_{12}s_{21}$$

B1 > 0 (Bodway [3])

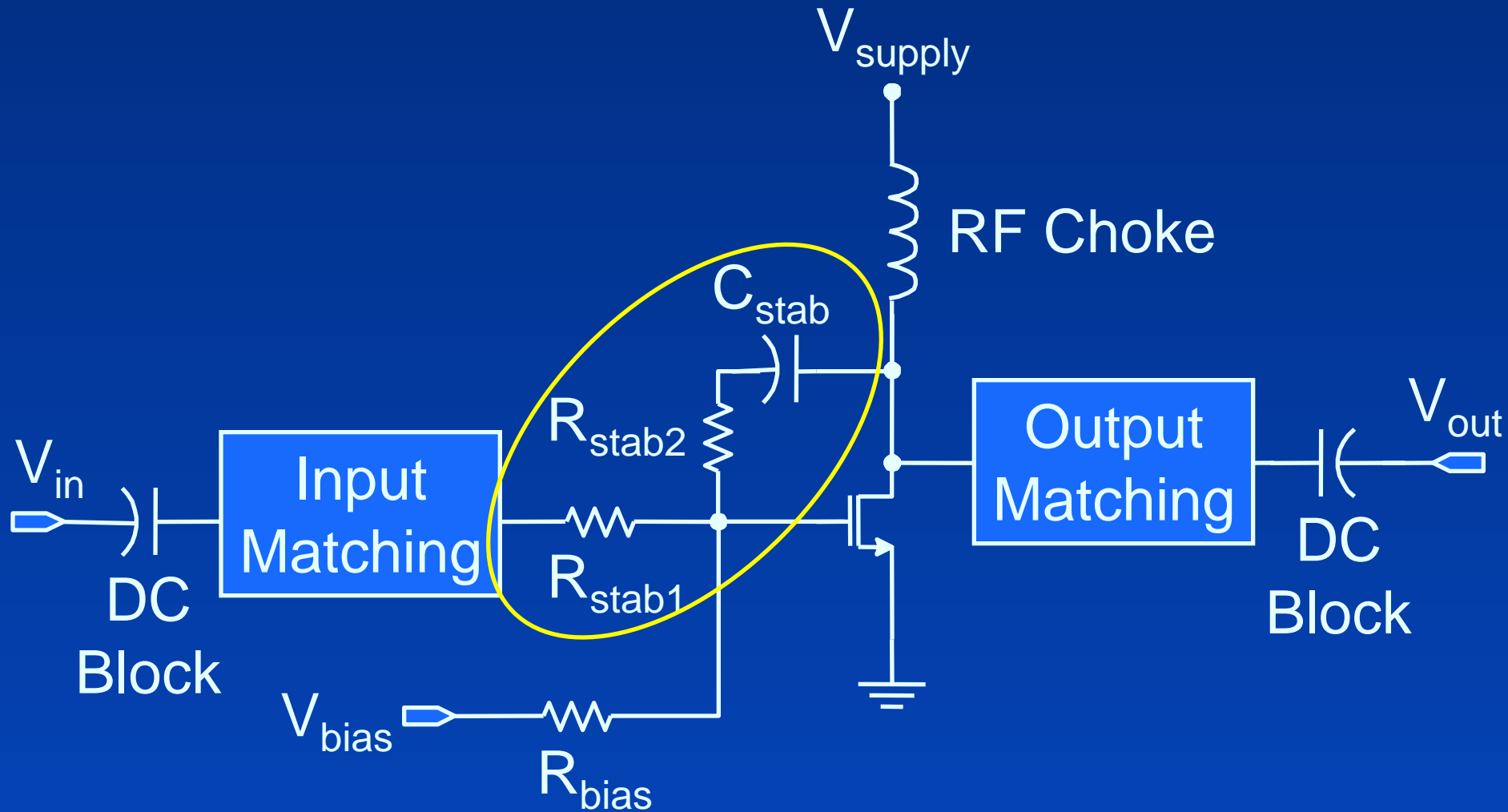
$$B_1 = 1 + |s_{11}|^2 - |s_{22}|^2 - |D|^2$$



# Stability circles



# Stabilized PA

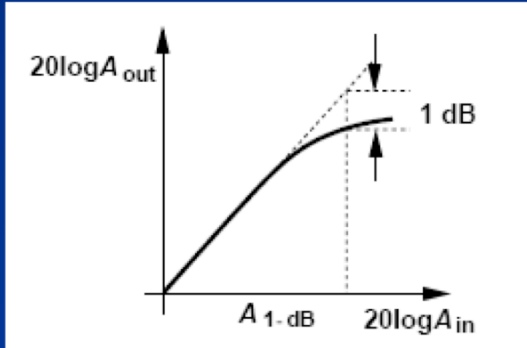


# Impedance matching networks

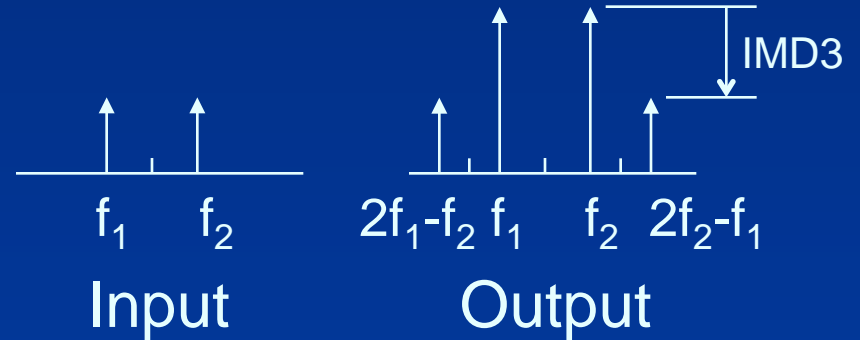
- For the determined  $R_{OPT}$ , find correspondent  $\Gamma_{IN}$  and choose  $\Gamma_S = \Gamma_{IN}^*$
- Choose a matching network for the output, in general low-pass (to attenuate harmonics), to transform the antenna impedance into  $R_{OPT}$  (Smith Chart [4])
- Choose a convenient matching network for the input so that the desired matching can be attained

# Linearity I – 2tone

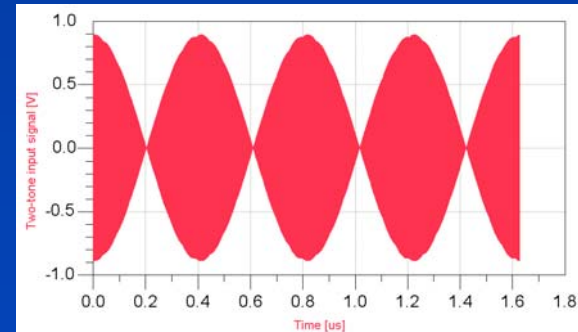
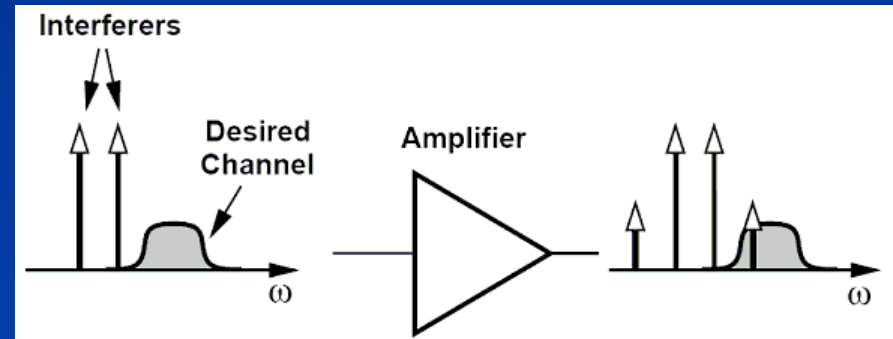
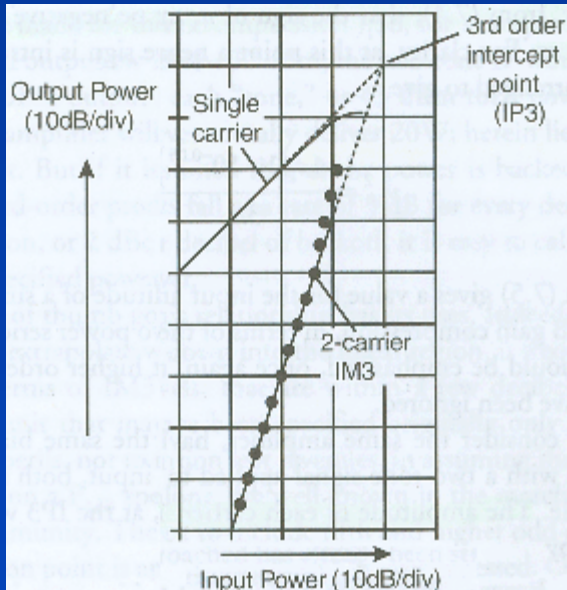
## 1-dB Compression Point



## 3<sup>rd</sup> Order Intermodulation Distortion (IMD3)

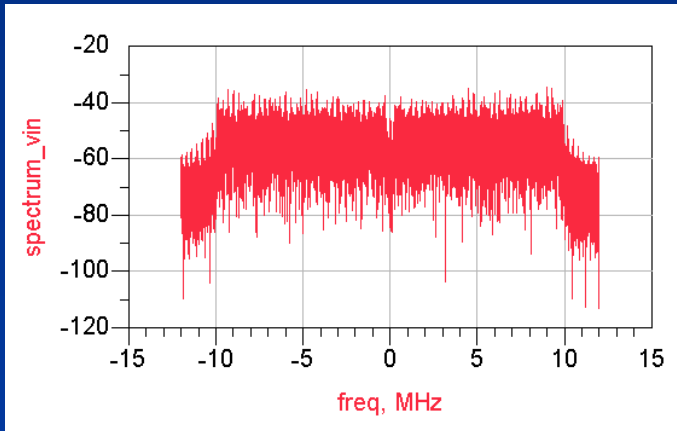


## 3<sup>rd</sup> Order Intercept Point

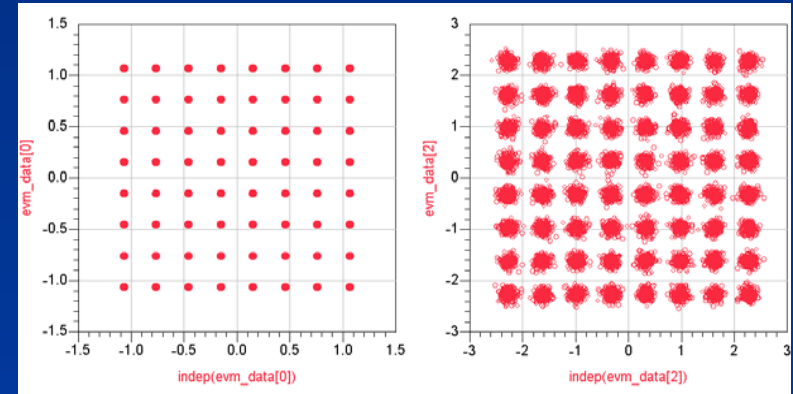


# Linearity II - OFDM

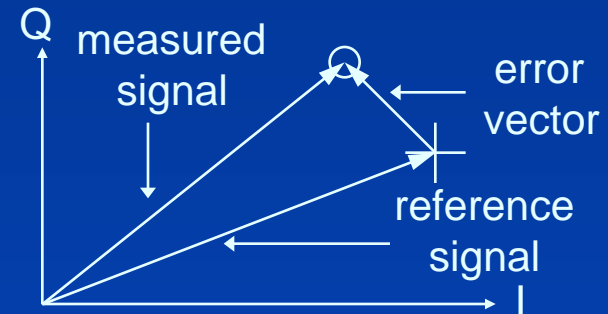
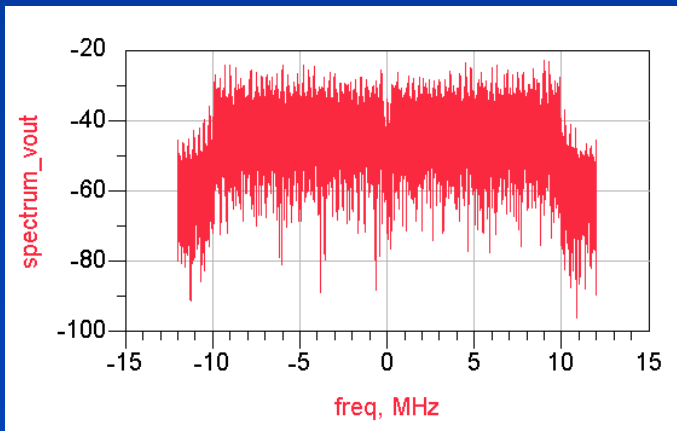
## Input OFDM spectrum



## Error Vector Magnitude

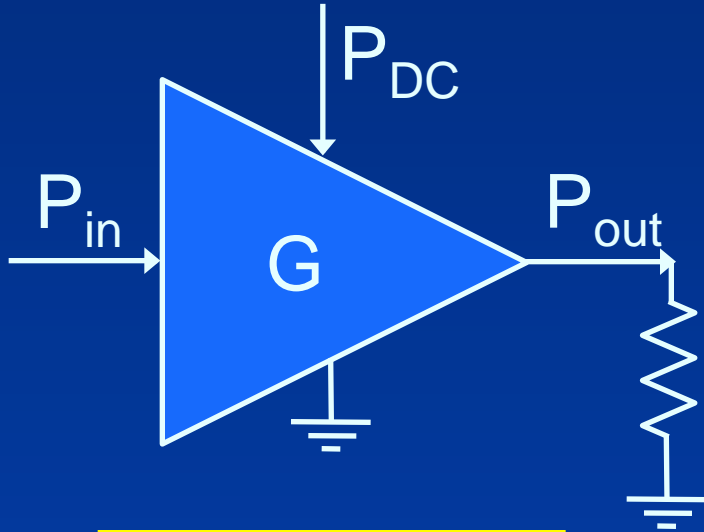


## Output OFDM spectrum



IEEE802.11a – EVM < -25dB (5.6%)  
OFDM, 64QAM, 54Mbps  
In general, **EVM < 3%**

# Efficiency



$$PAE = \frac{P_{OUT} - P_{IN}}{P_{DC}}$$

$$\eta = \frac{P_{OUT}}{P_{DC}}$$

$$P_{OUT} = G \cdot P_{IN}$$

$$PAE = \eta_D \cdot \left(1 - \frac{1}{G}\right)$$

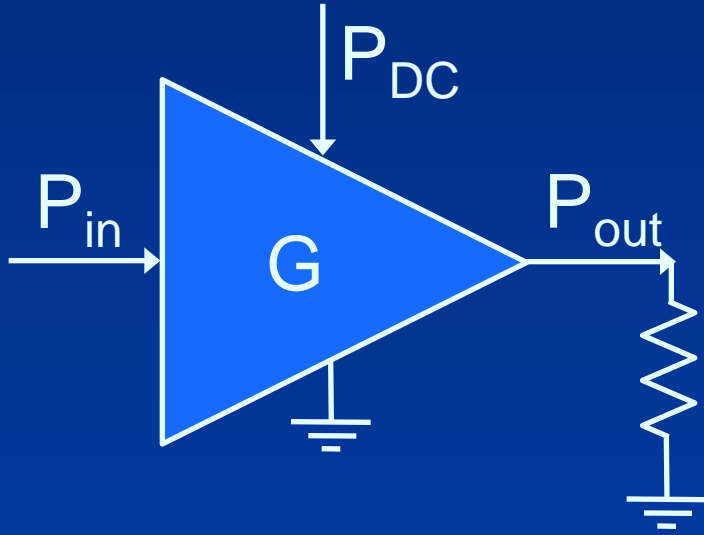
## Class A PA:

- Max efficiency with  $P_{OUT\_MAX}$
- Consumes power even without input signal
- Efficiency depends also on gain

# Scenario

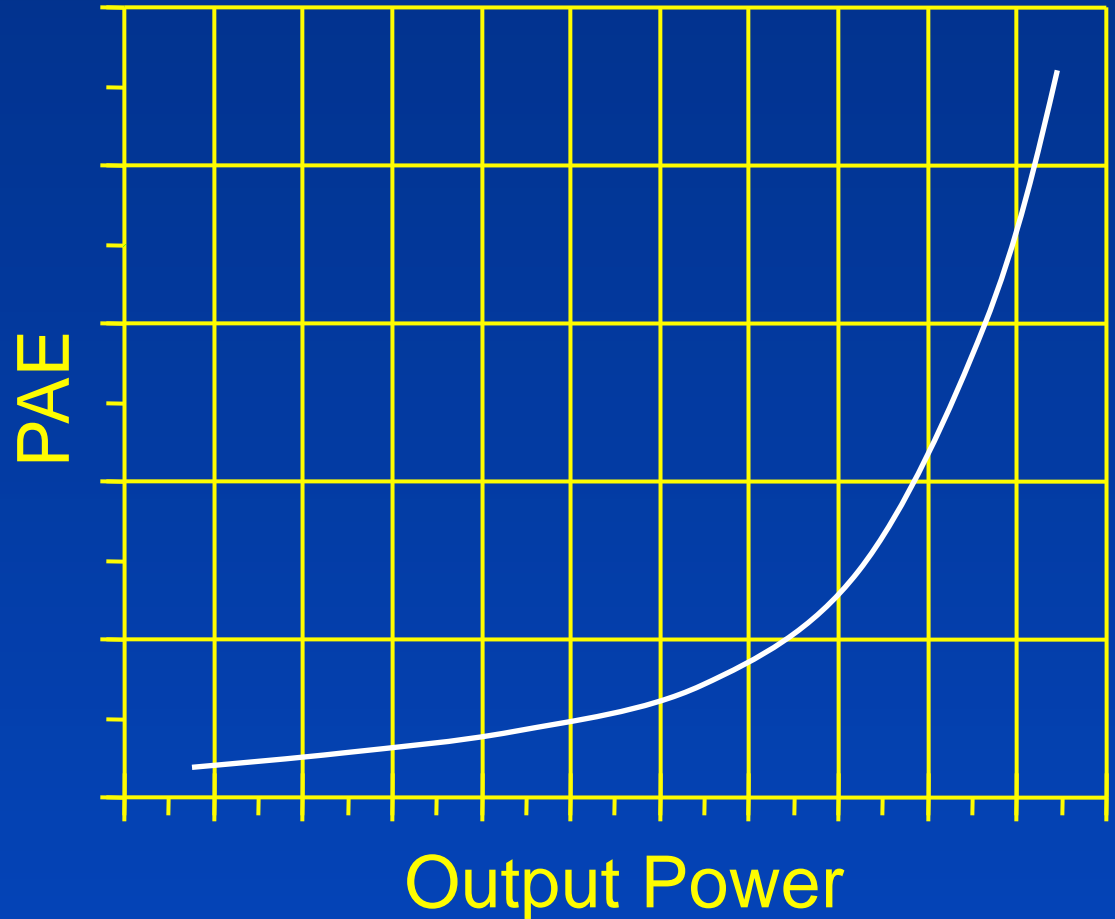
- Mobile devices require high efficiency circuits
- Applications such as WLAN (variable envelope) requires high linearity PAs
- RF power amplifiers are power hungry devices
- High efficiency PA means low linearity PA

# Improving efficiency...

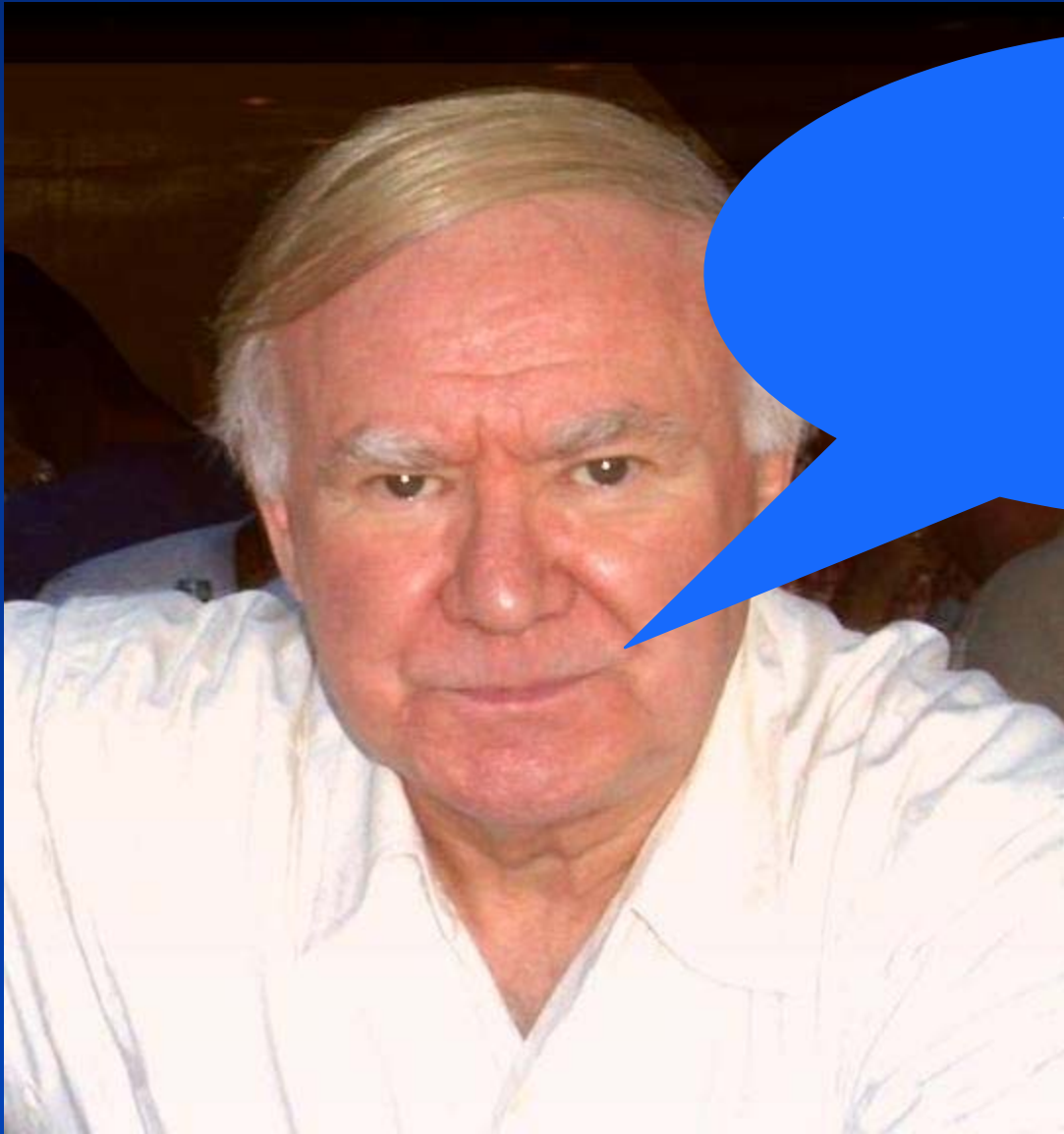


$$PAE = \frac{P_{OUT} - P_{IN}}{P_{DC}}$$

$$P_{DC} = V_{DD} \cdot I_{DD}$$

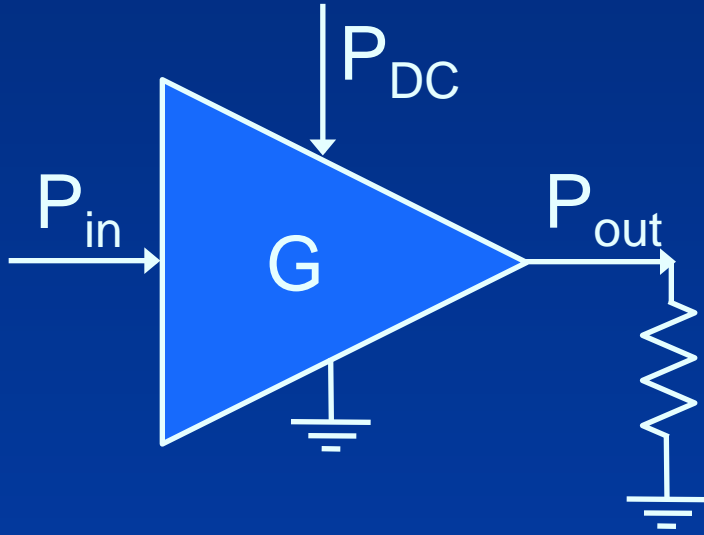






**What if ...?**

# What if....?



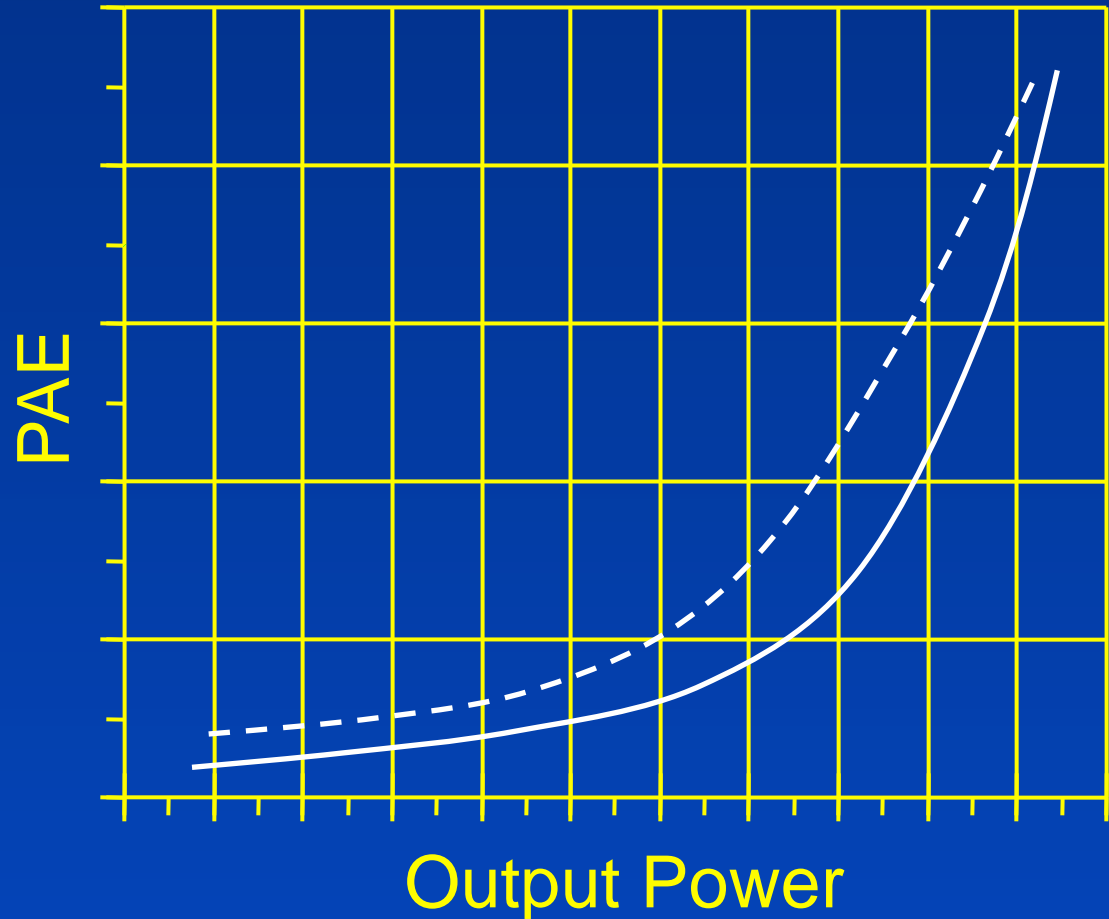
$$PAE = \frac{P_{OUT} - P_{IN}}{P_{DC}}$$

$$P_{DC} = V_{DD} \cdot I_{DD}$$

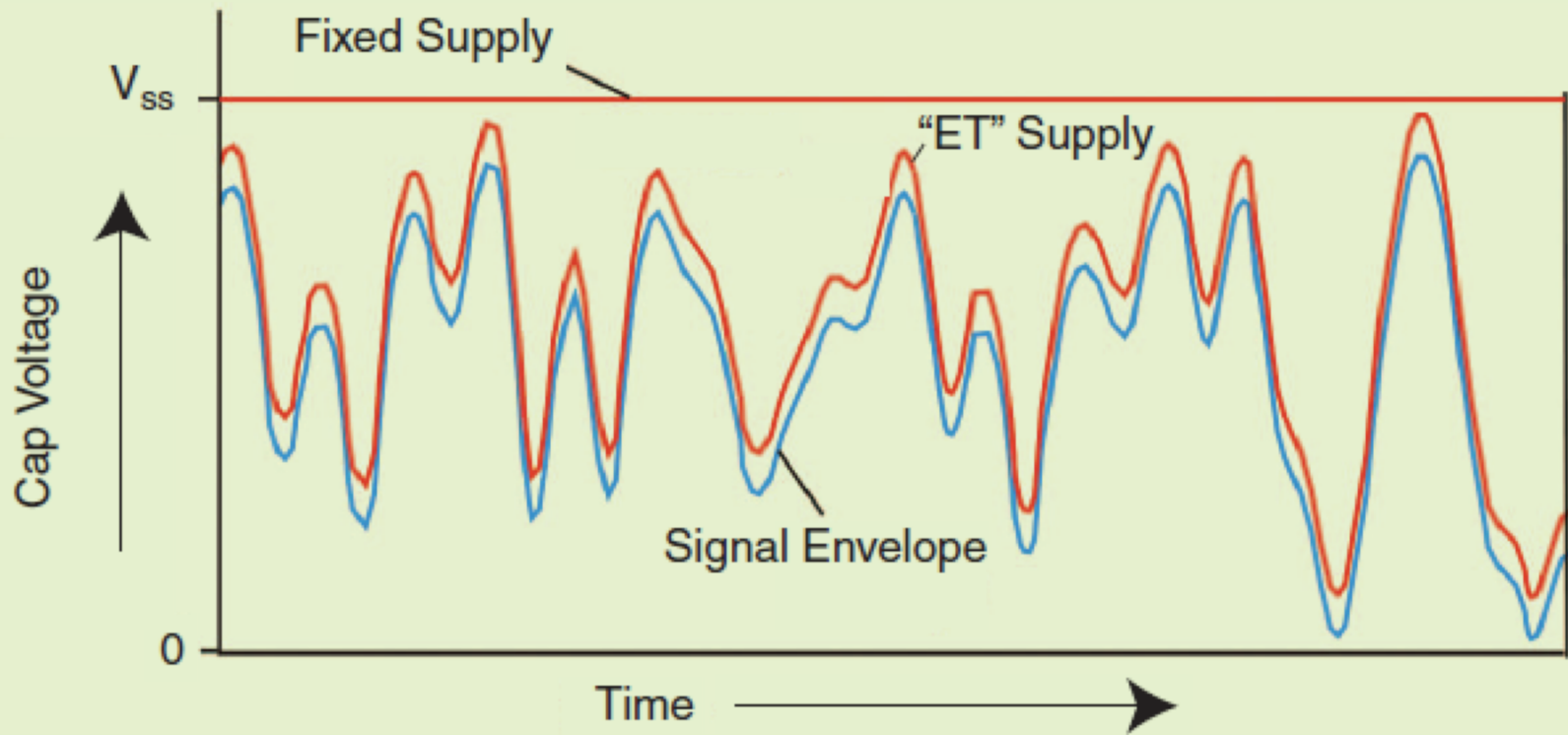
Low output power:  $V_{DC} \downarrow$

High output power:  $V_{DC} \uparrow$

--- Dynamic Supply  
— Constant VDD



# Dynamic Supply

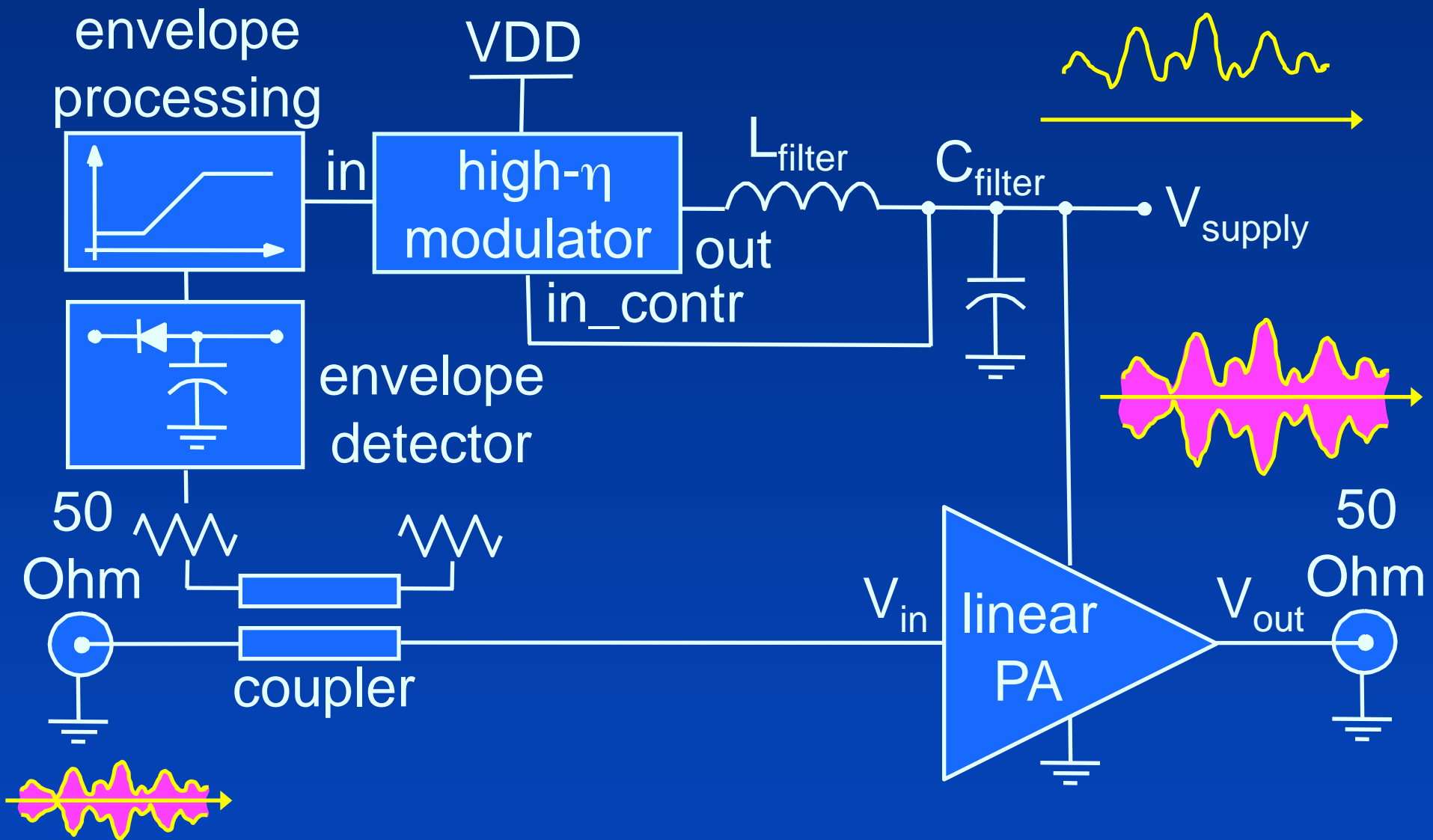


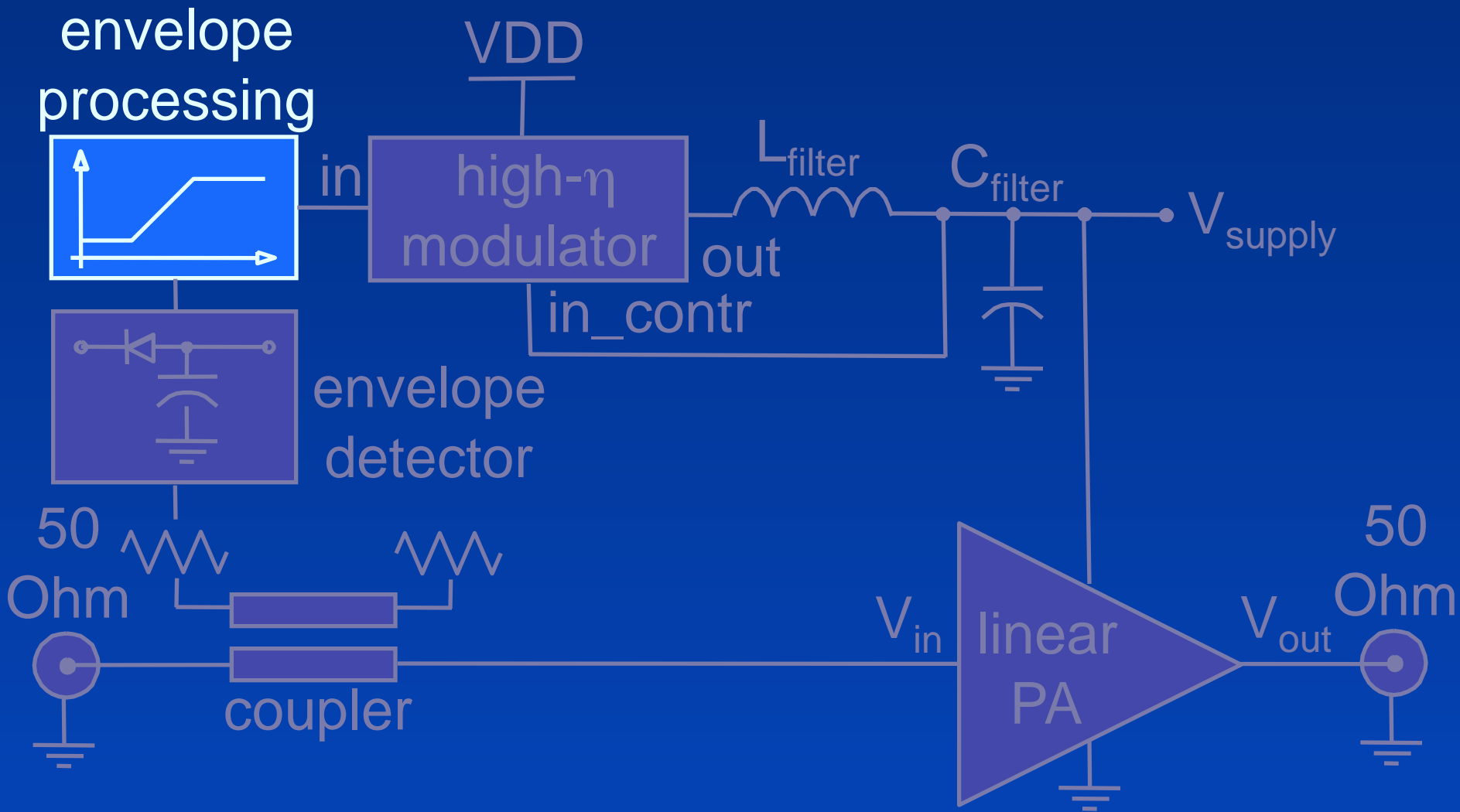
From Cripps, Microwave Magazine Oct-2010

# Articles about enhancement techniques

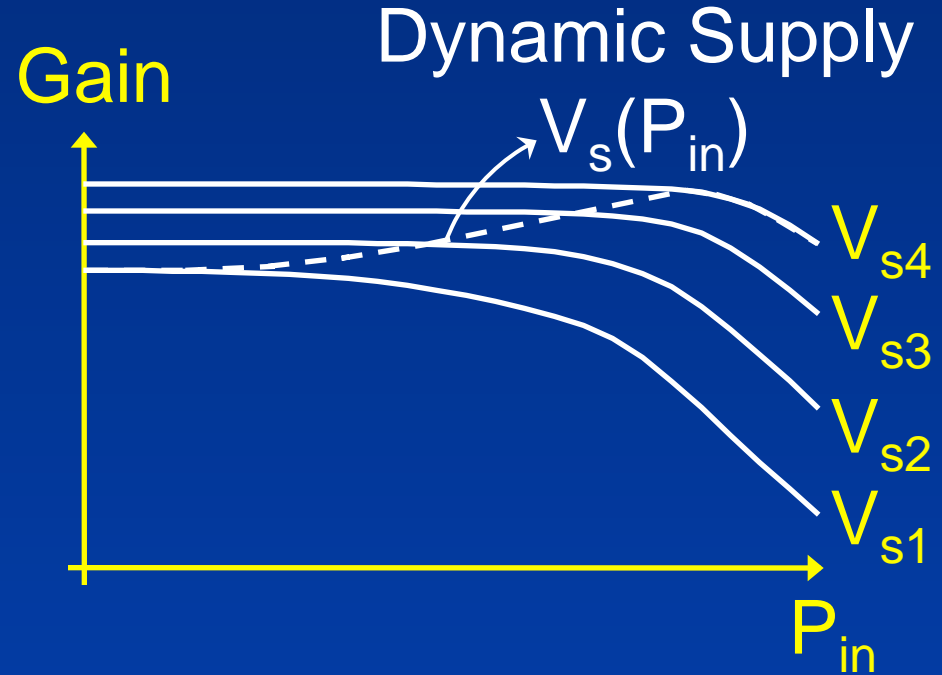
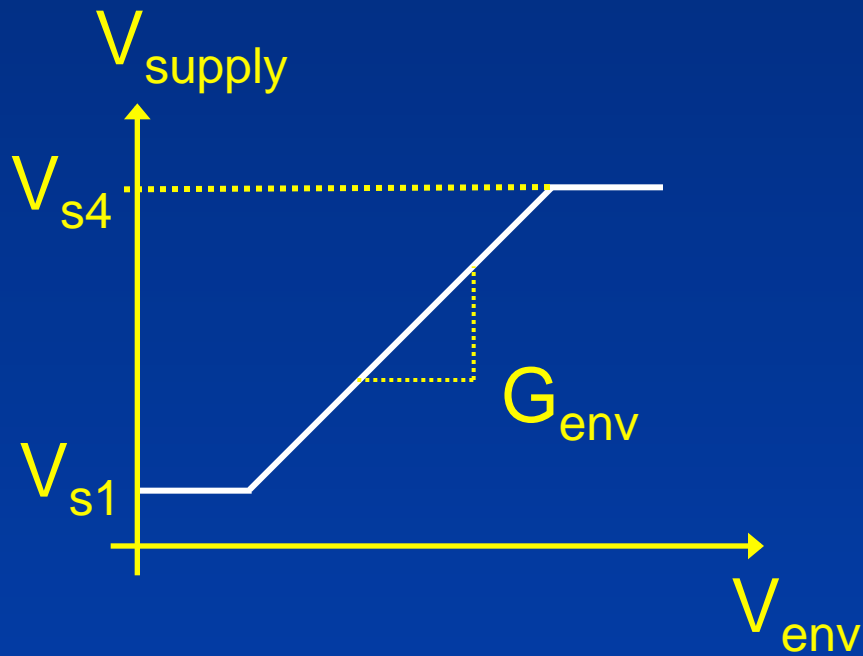
- Dynamic Supply:
  - Hanington [5], 1999 (T-MTT)
  - Schlumpf [1], 2004 (JSSC)
  - Minnis [7], 2009 (T-CAS-1)
  - Larson [10], 2008 (CICC)
  - Jeong [9], 2009 (T-MTT)
- EER:
  - Chen [6], 2004 (MTT-S)

# Dynamic Supply PA Block Diagram





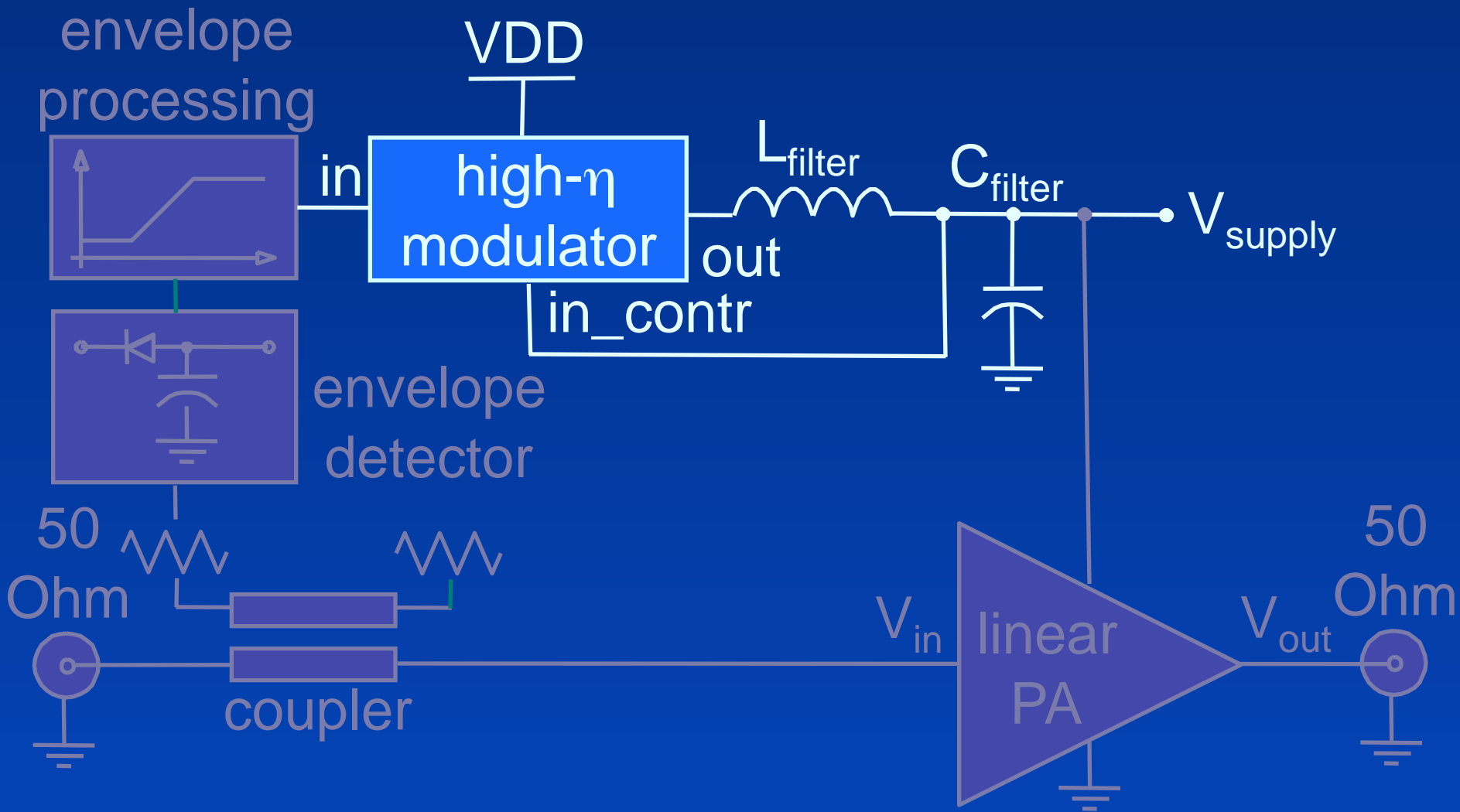
# Envelope processing



$$G_{env} \cdot |V_{in}| + V_{knee} < V_{s1} \rightarrow V_s(P_{in}) = V_{s1}$$

$$V_{s1} \leq G_{env} \cdot |V_{in}| + V_{knee} \leq V_{s4} \rightarrow V_s(P_{in}) = G_{env} \cdot |V_{in}| + V_{knee}$$

$$G_{env} \cdot |V_{in}| + V_{knee} \geq V_{s4} \rightarrow V_s(P_{in}) = V_{s4}$$

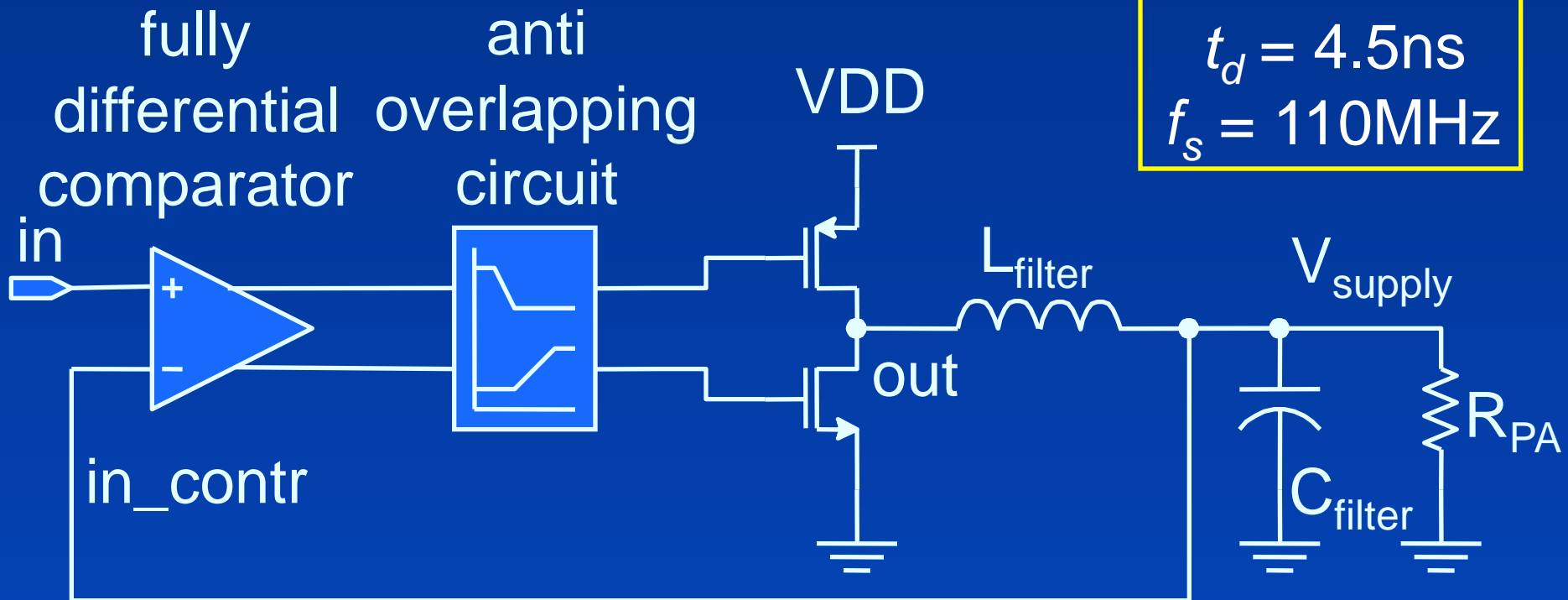


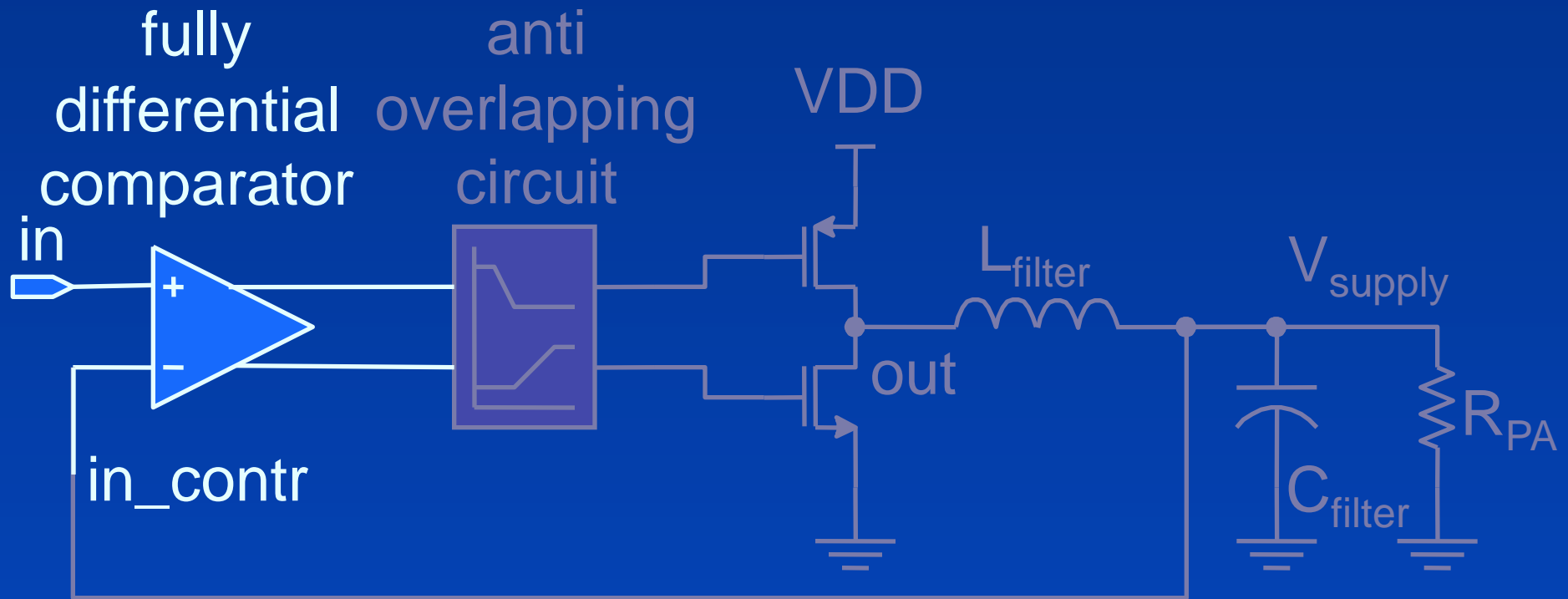


# High-Efficiency Modulator

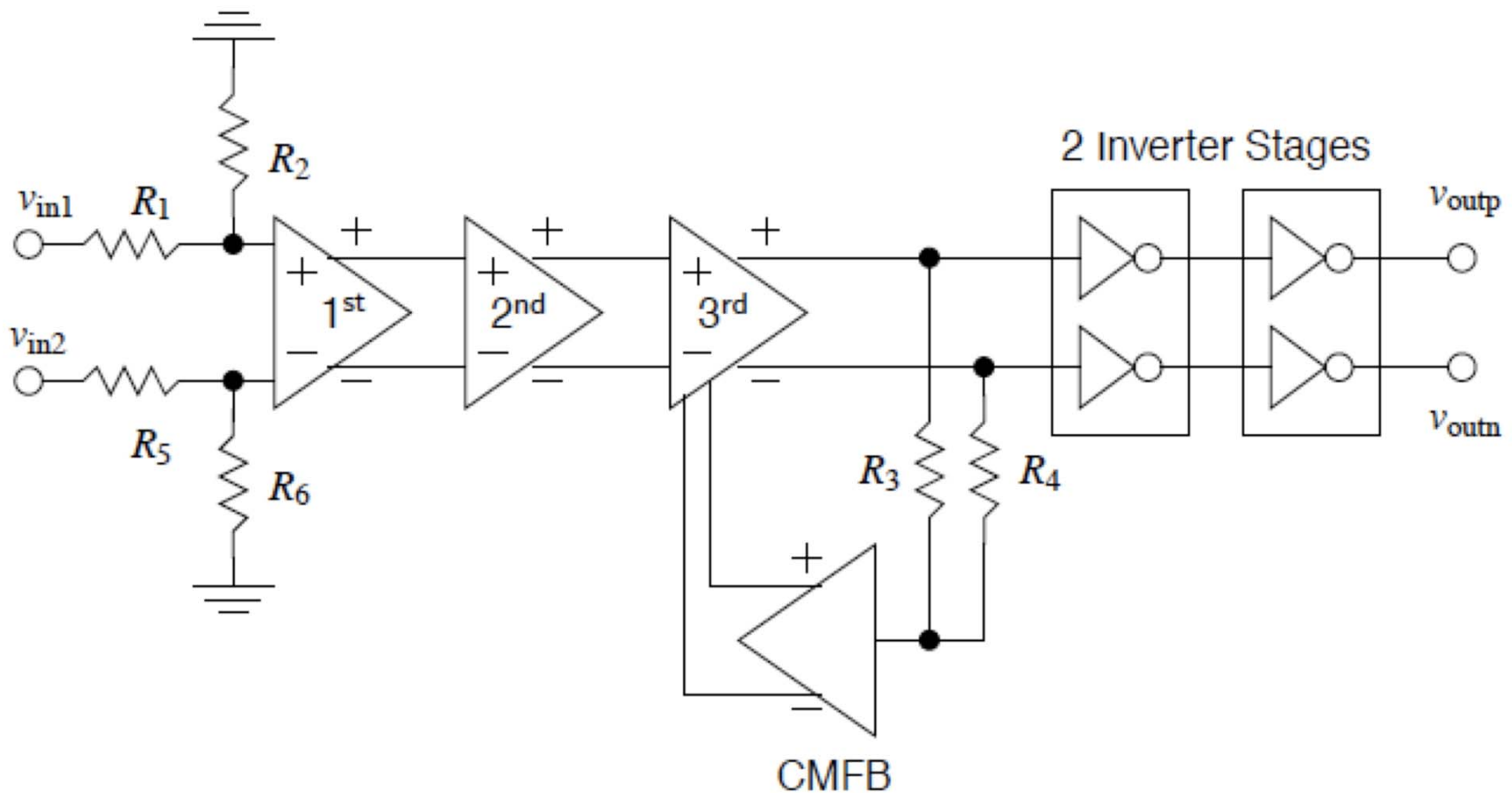
$$\eta = 86\%$$

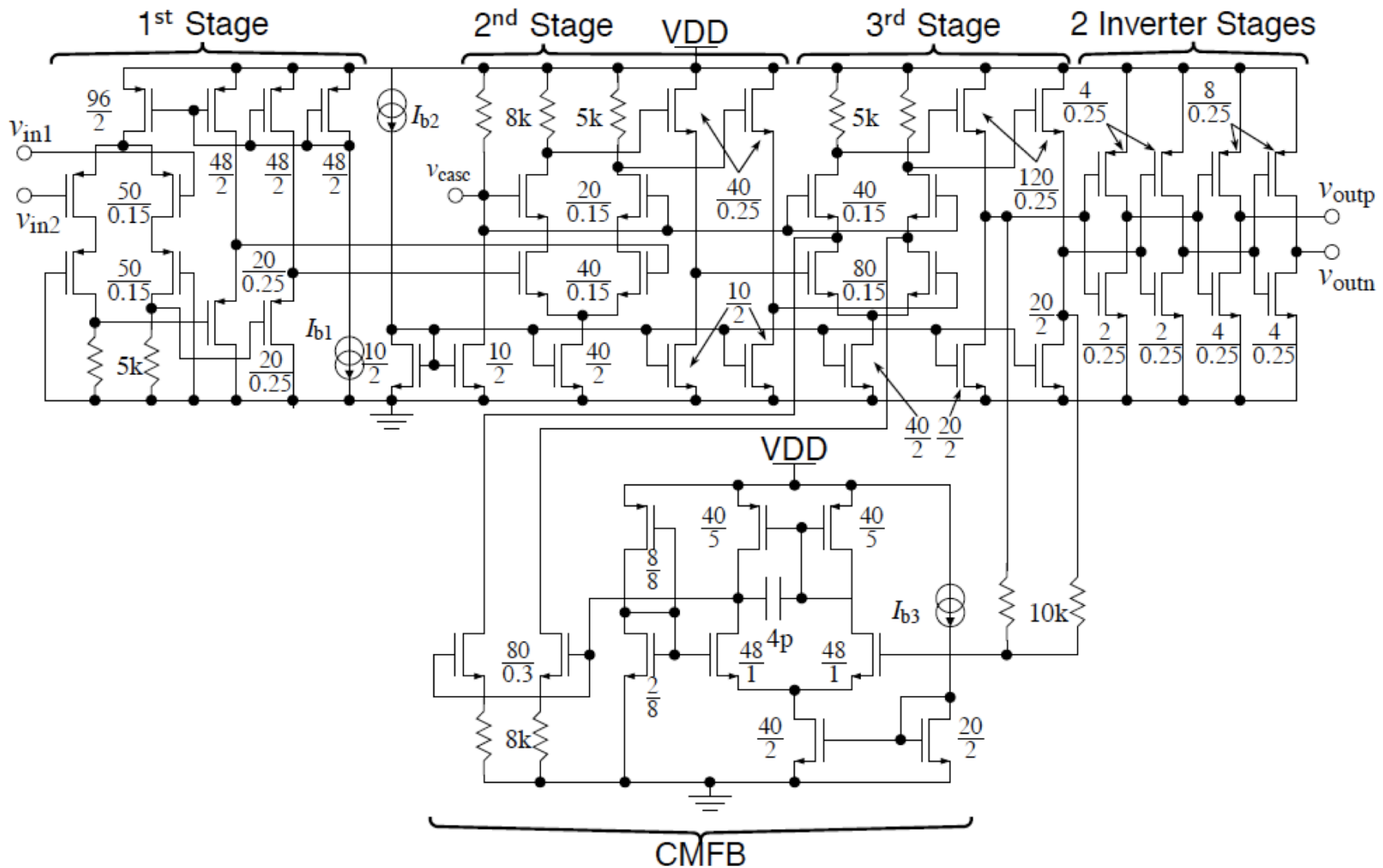
$$f_s \cdot t_d \cdot 360^\circ + \varphi_{LC}(f_s) = 180^\circ$$

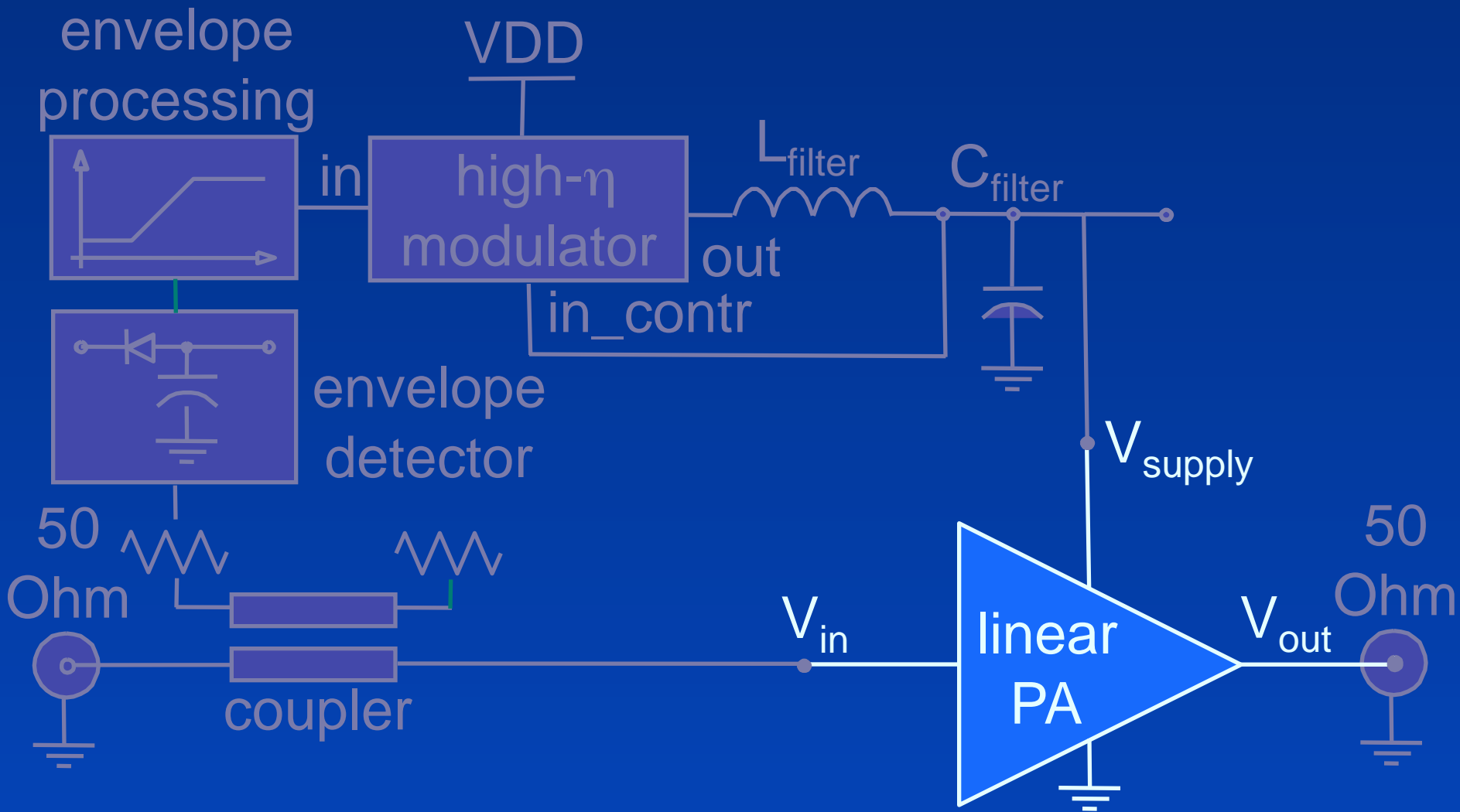




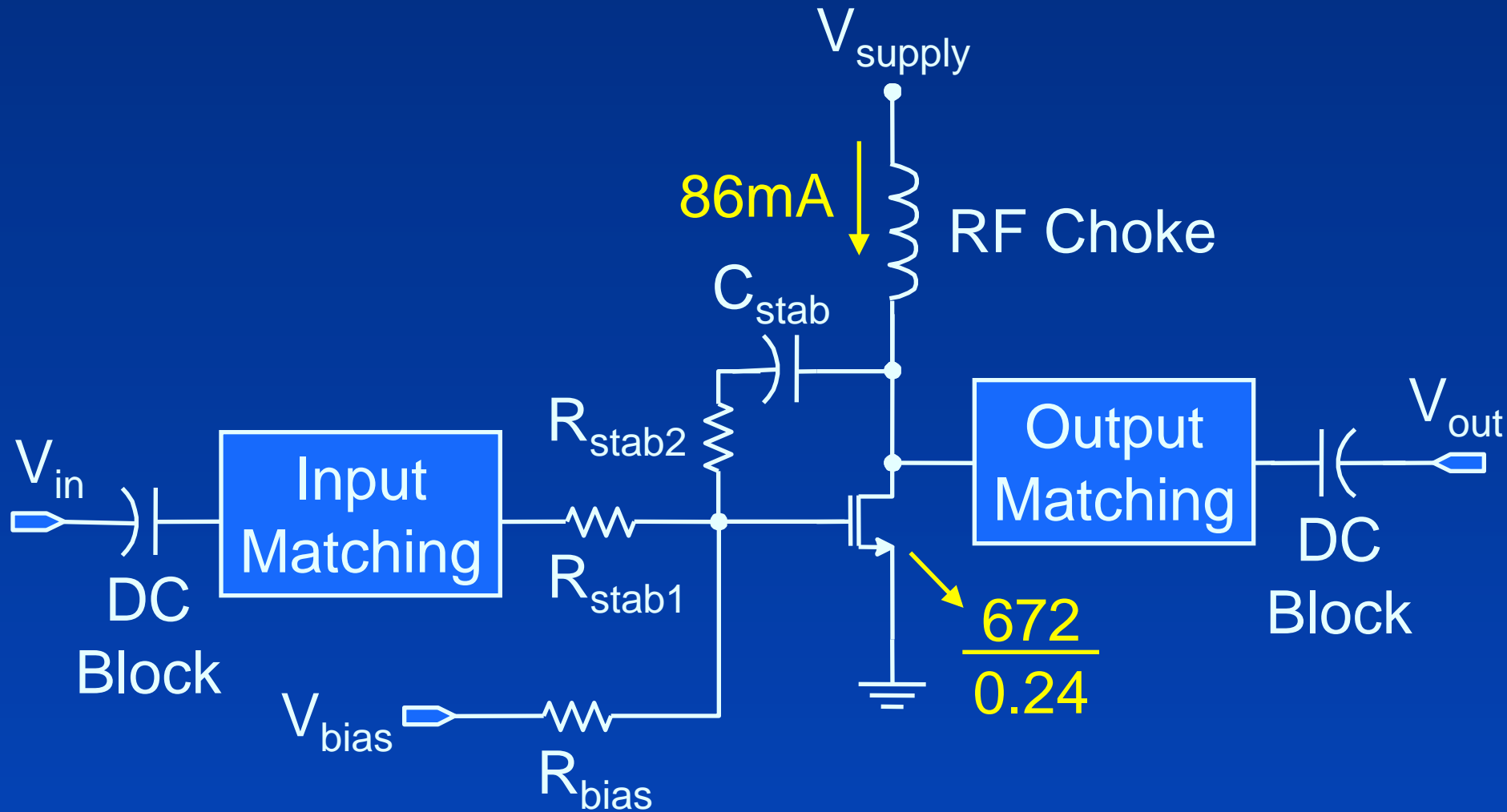
# High-Speed Comparator



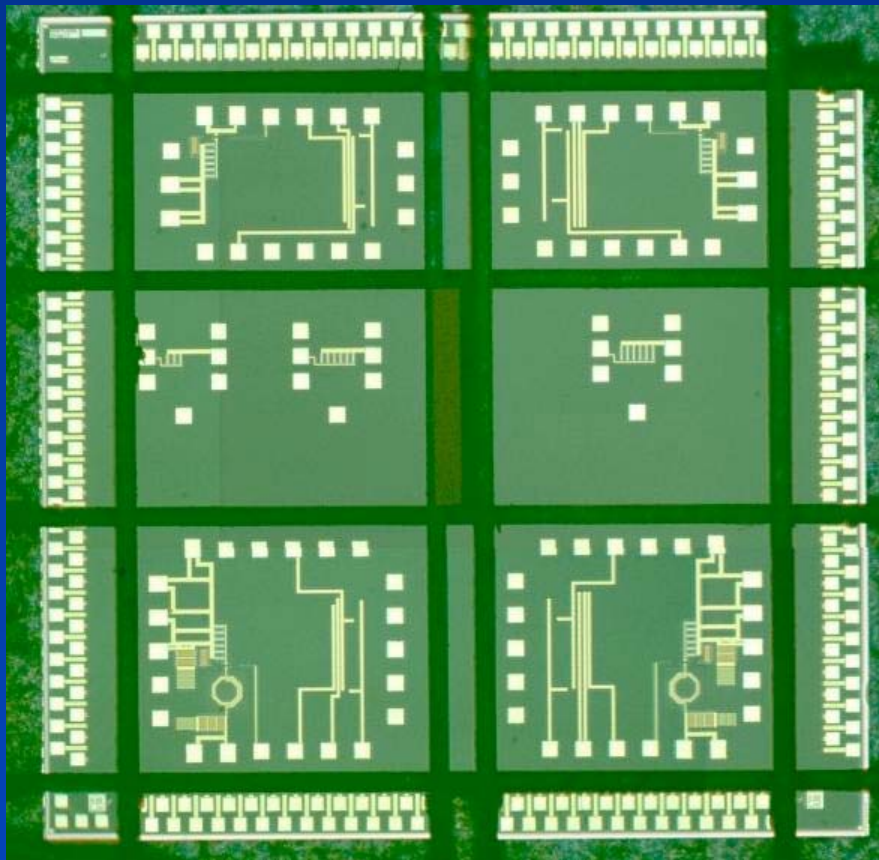
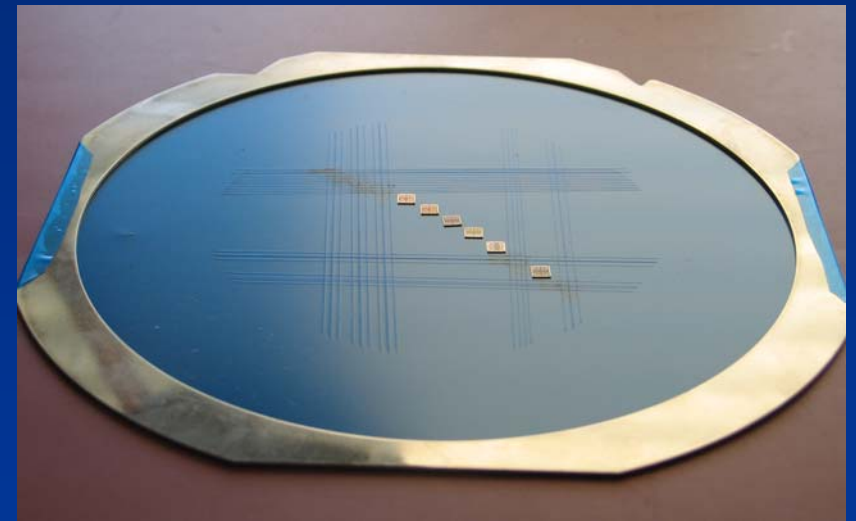




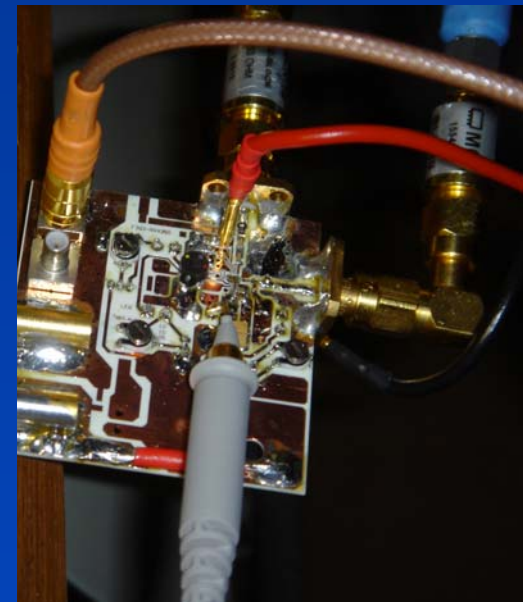
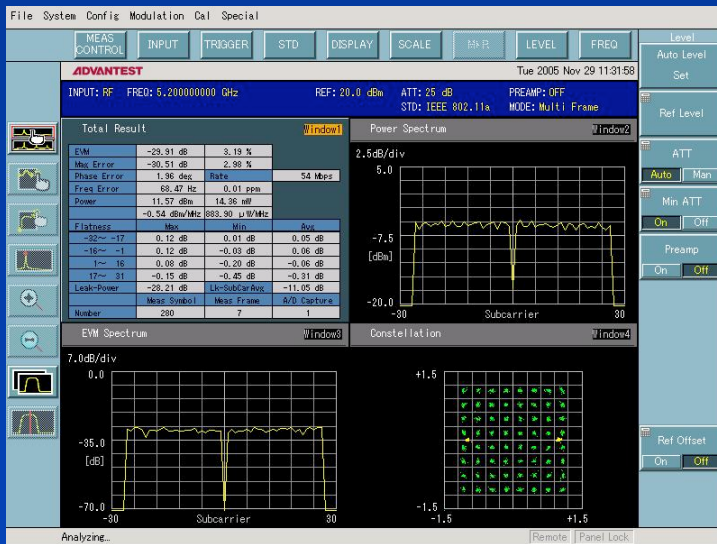
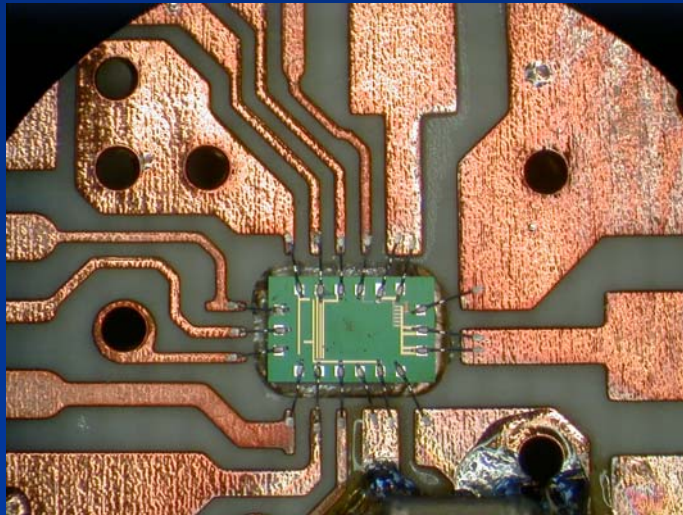
# The RF Power Amplifier



# Measurements I

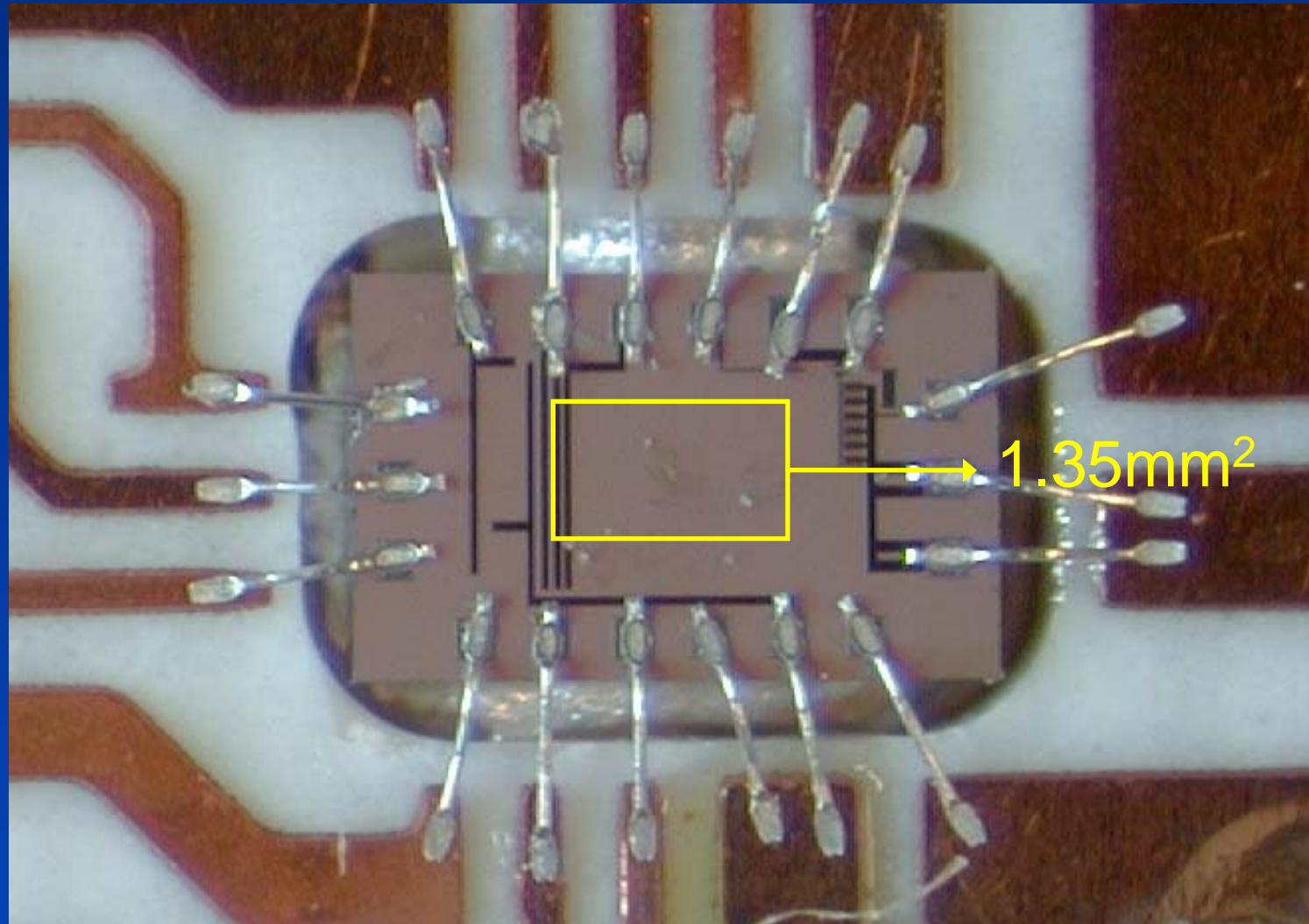


# Measurements II

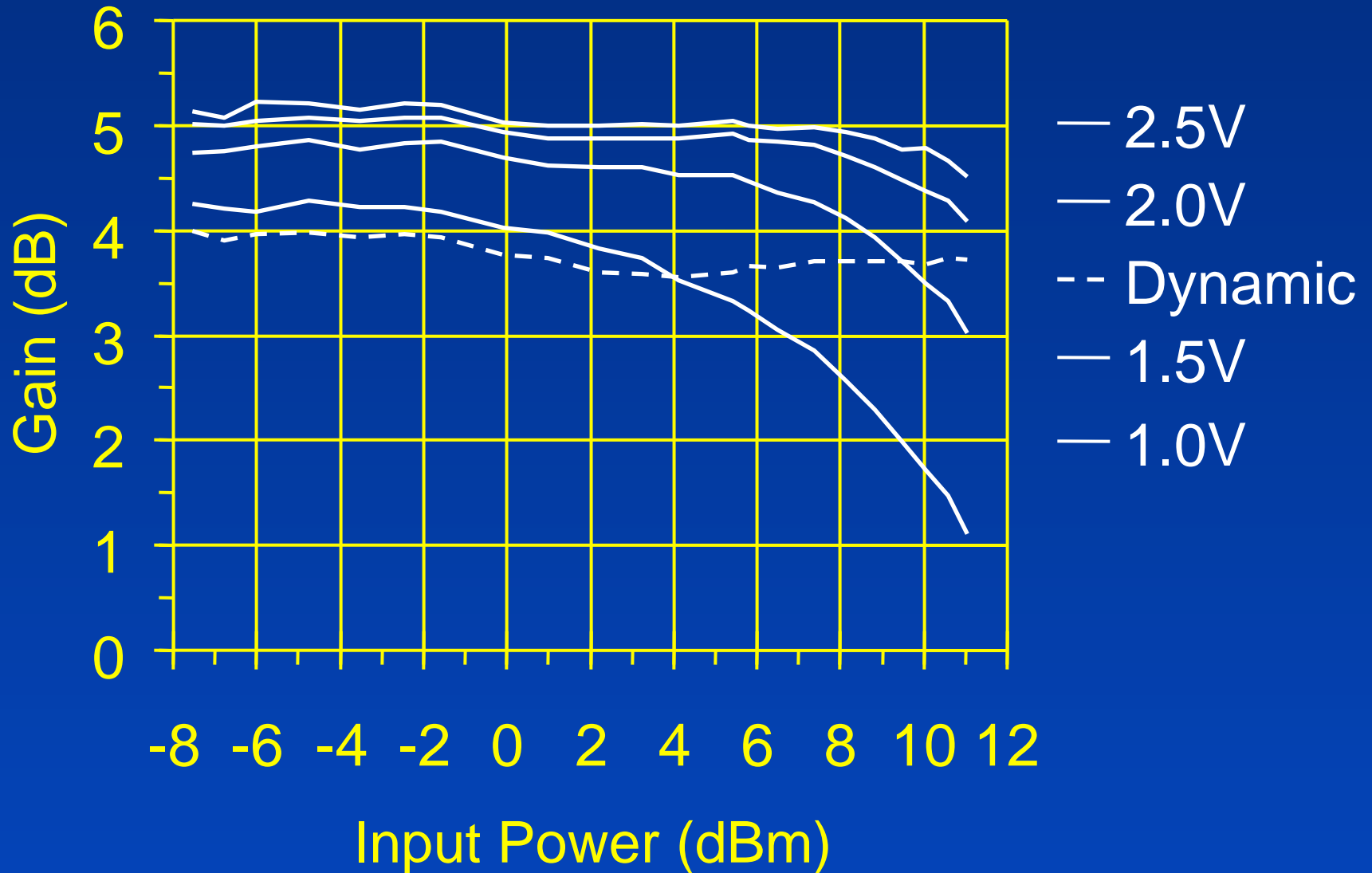




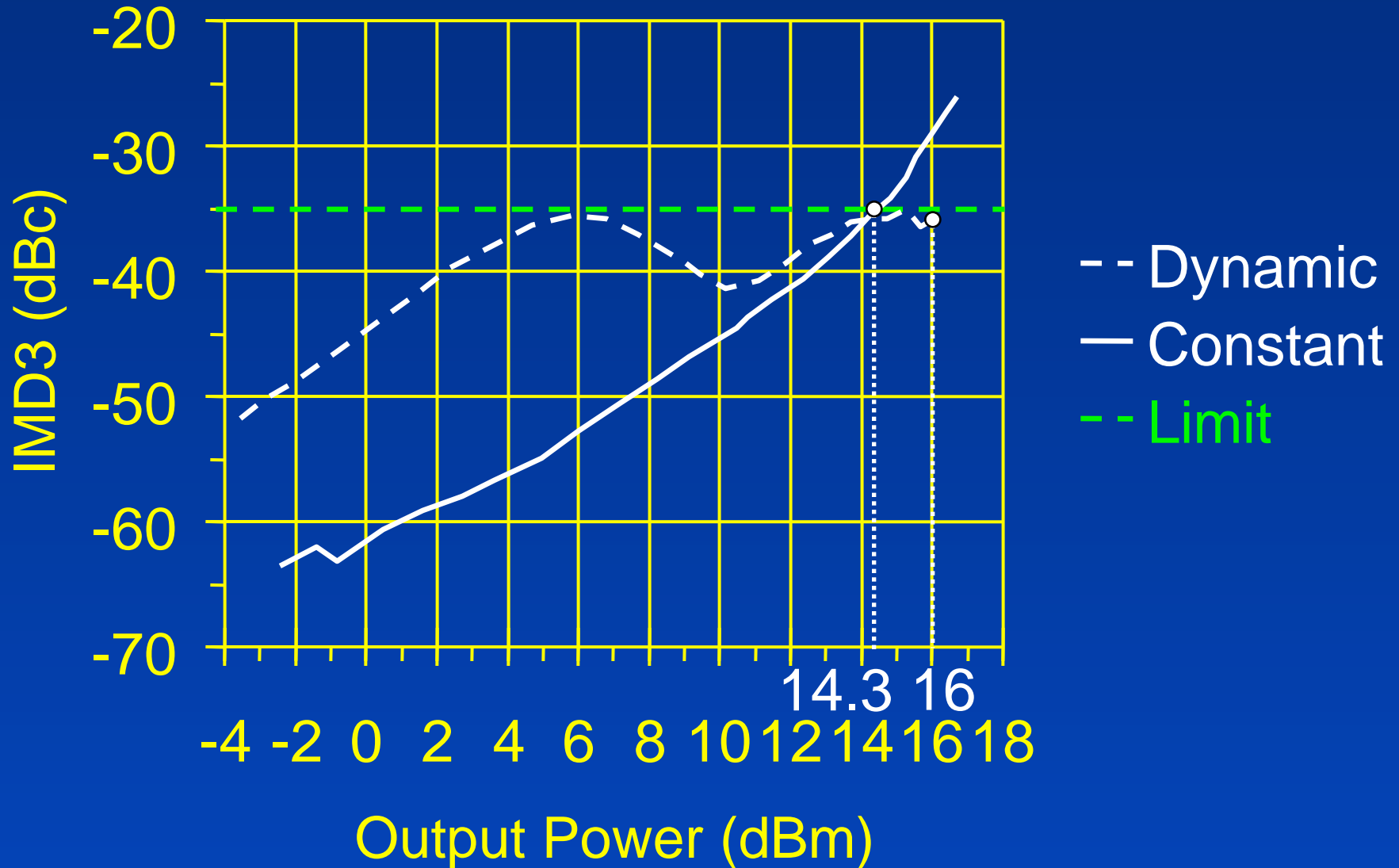
# Measurement Results [8]



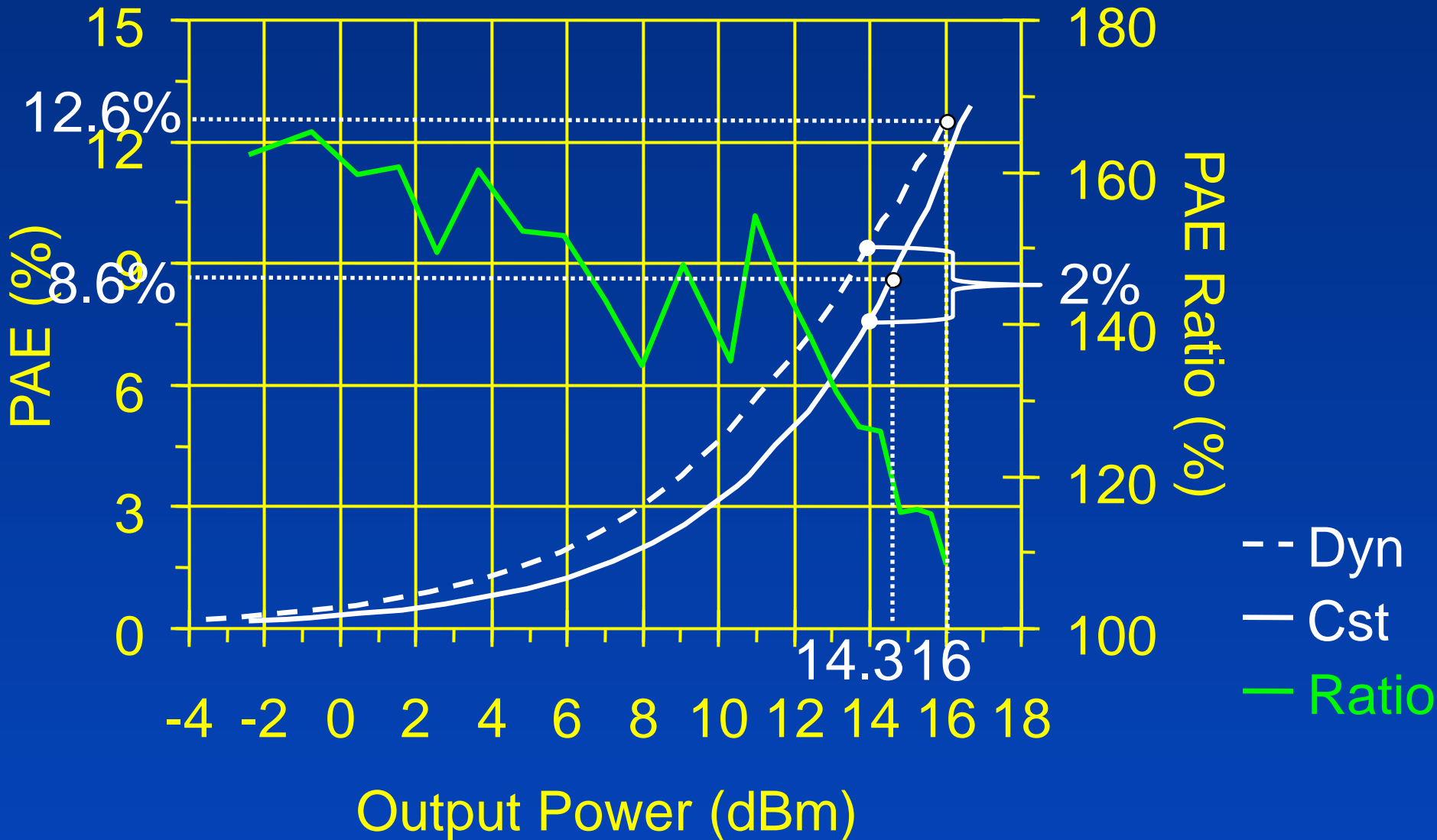
# Gain vs. Input Power 5.2GHz



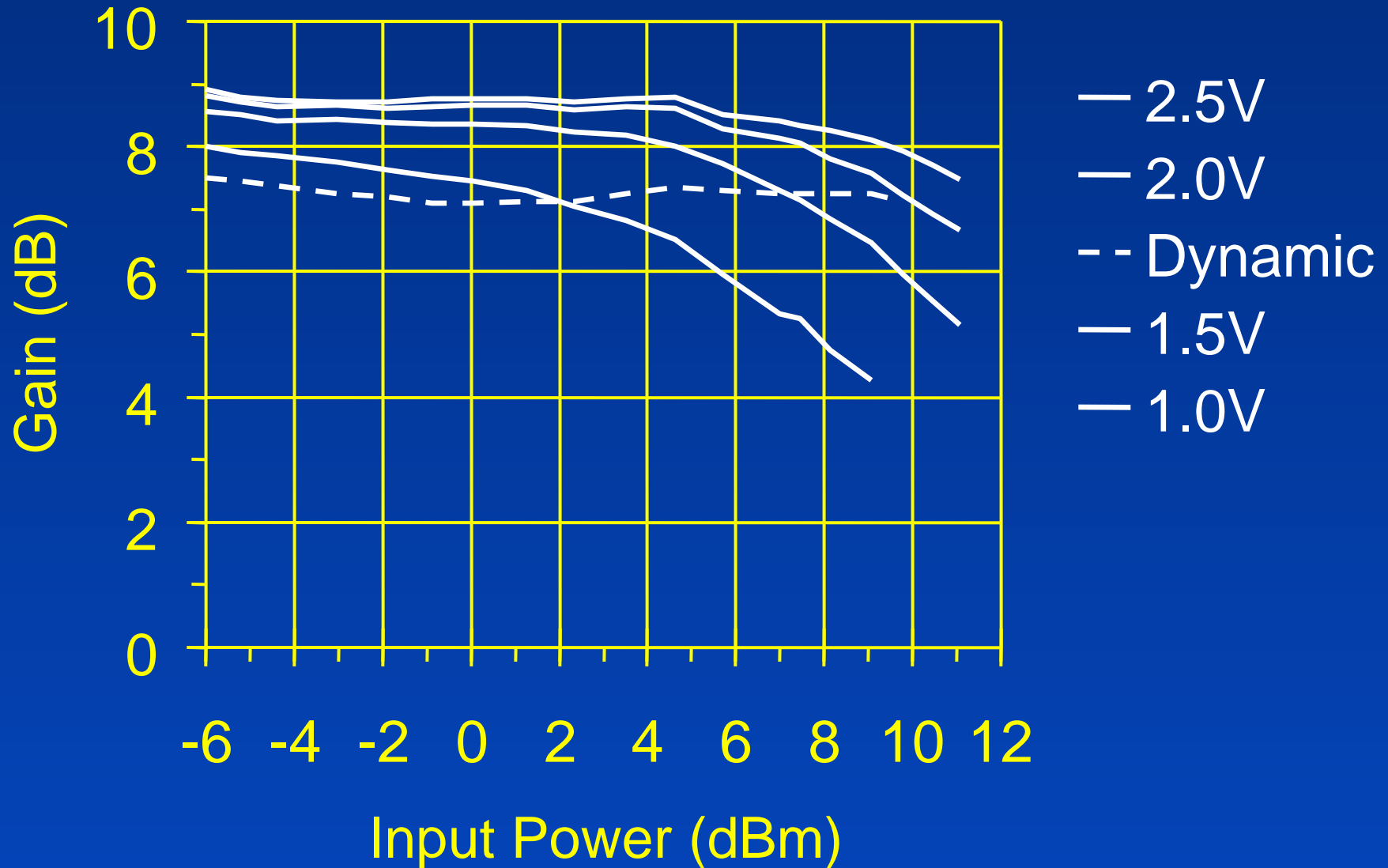
# IMD3 vs. Output Power 5.2GHz



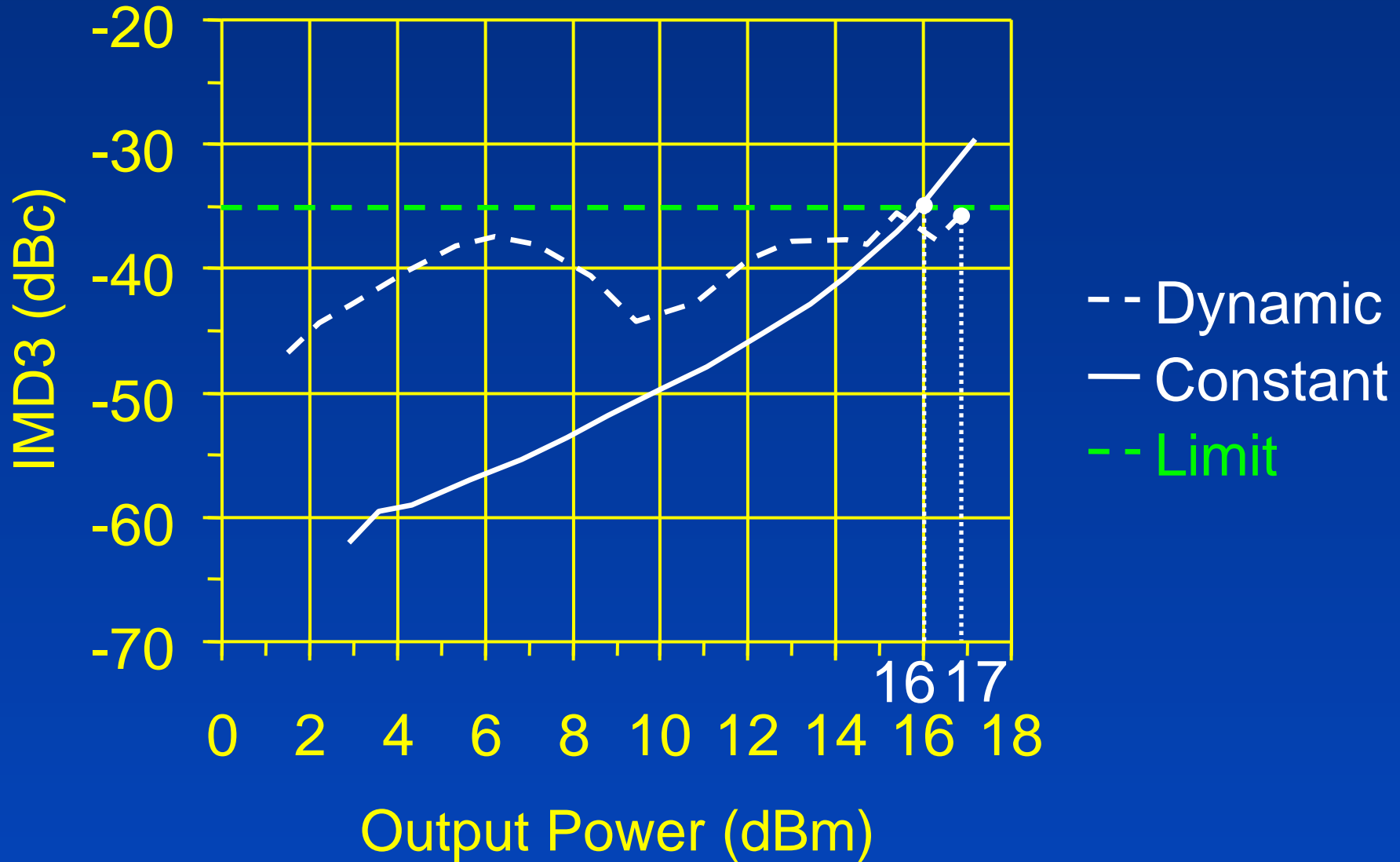
# Efficiency vs. Output Power 5.2GHz



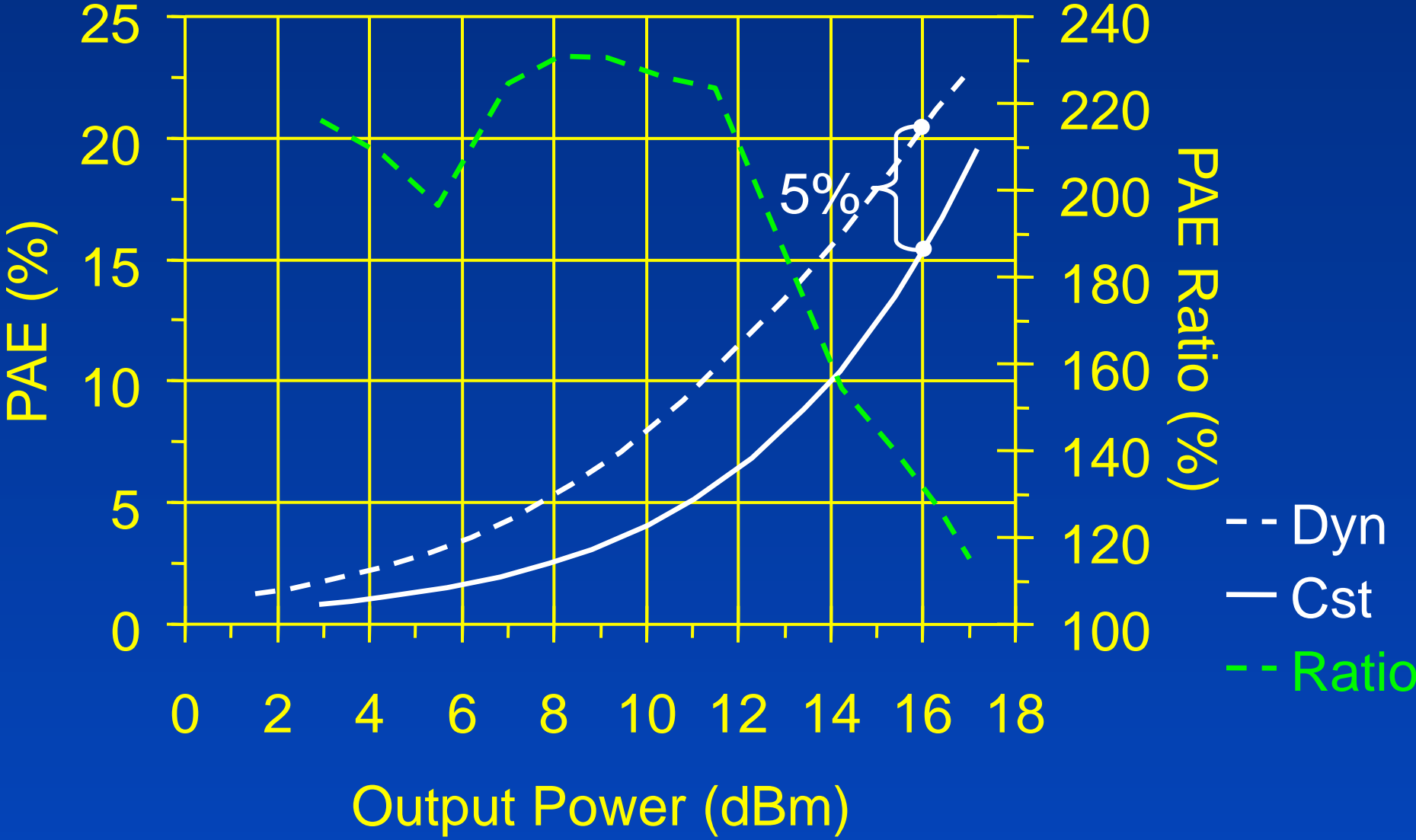
# Gain vs. Input Power 2.4GHz



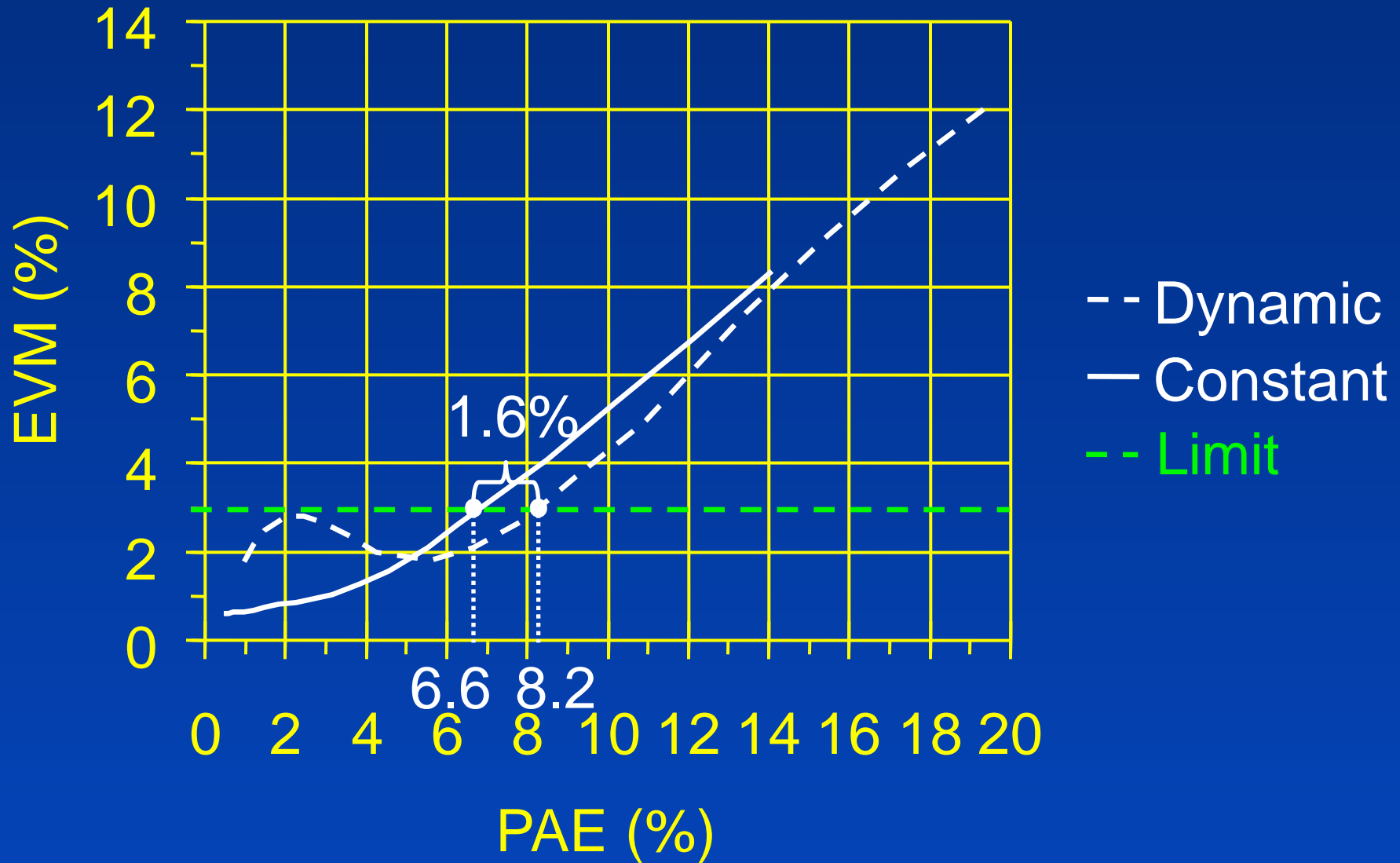
# IMD3 vs. Output Power 2.4GHz



# Efficiency vs. Output Power 2.4GHz



# EVM vs. Efficiency 2.4GHz





# Summary & Conclusion

- RF power amplifier basics
- Dynamic supply principle
- Modulator and PA circuits
- Improvement needed for WLAN application
- Efficiency enhancement verified through measurement results at 2.4 and 5.2GHz

# References

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